Simulink[®] Design Optimization[™] Getting Started Guide

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Simulink[®] Design Optimization[™] Getting Started Guide

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Simulink Design Optimization Product Description

Analyze model sensitivity and tune model parameters

Simulink Design Optimization provides functions, interactive tools, and blocks for analyzing and tuning model parameters. You can determine the model's sensitivity, fit the model to test data, and tune it to meet requirements. Using techniques like Monte Carlo simulation and Design of Experiments, you can explore your design space and calculate parameter influence on model behavior.

Simulink Design Optimization helps you increase model accuracy. You can preprocess test data, automatically estimate model parameters such as friction and aerodynamic coefficients, and validate the estimation results.

To improve system design characteristics such as response time, bandwidth, and energy consumption, you can jointly optimize physical plant parameters and algorithmic or controller gains. These parameters can be tuned to meet time-domain and frequency-domain requirements, such as overshoot and phase margin, and custom requirements.

Key Features

- Parameter estimation from test data
- Parameter tuning to meet time-domain, frequency-domain, and custom requirements
- Design exploration and sensitivity analysis
- Graphical requirement specification and optimization progress monitoring
- Robust design optimization, accounting for parameter variation or uncertainty

Optimization Support for Simulink Models Using Third-Party Applications

You can use Simulink Design Optimization software to optimize Simulink models that invoke thirdparty simulation tools or contain legacy simulation code. To do so, use the S-Function block in Simulink. When using the command-line functions, use MATLAB[®] MEX functions.

References

Cherian, V., Shenoy, R., Stothert, A., Shriver, J. et al., "Model-Based Design of a SUV Anti-rollover Control System" SAE Technical Paper 2008-01-0579, 2008, doi:10.4271/2008-01-0579.

See Also

More About

• "Choosing MEX Applications"

Ways to Speed Up Design Optimization Tasks

You can use the following ways to speed up parameter estimation, response optimization, and sensitivity analysis tasks:

- Parallel computing
- Fast restart mode
- Accelerator mode

You can use a combination of these, but depending on the limitations associated with each, you may or may not see an increase in speed. For example, you can use parallel computing and fast restart together to speed up optimization. However, you do not see an increase in speed compared to using only parallel computing if the compilation phase of your model is short.

Speed Up Using Parallel Computing

You can use Parallel Computing Toolbox[™] software to speed up parameter estimation, response optimization, and sensitivity analysis. When you use parallel computing, the software distributes the independent simulations on multiple MATLAB sessions. Thus, the simulations run in parallel, which reduces the optimization time.

Using parallel computing may reduce the optimization time in the following cases:

- The model contains many parameters to optimize, and you use the Gradient descent or Nonlinear least squares method.
- The Pattern search method is selected as the optimization method.
- The model contains many uncertain parameters and uncertain parameter values.
- The model is complex and takes a long time to simulate.

You can use parallel computing in the **Parameter Estimator**, **Response Optimizer**, and **Sensitivity Analyzer** apps, or at the command line. For more information, see "Use Parallel Computing for Parameter Estimation", "Use Parallel Computing for Response Optimization", and "Use Parallel Computing for Sensitivity Analysis".

Speed Up Using Fast Restart Mode

You can use the fast restart feature of Simulink to speed up design optimization of tunable parameters of a model.

Fast restart enables you to perform iterative simulations without compiling a model or terminating the simulation each time. Using fast restart, you compile a model only once. You can then tune parameters and simulate the model again without spending time on compiling. Fast restart associates multiple simulation phases with a single compile phase to make iterative simulations more efficient. You see a speedup of design optimization tasks using fast restart in models that have a long compilation phase. See "How Fast Restart Improves Iterative Simulations".

When you enable fast restart, you can only change tunable properties of the model during simulation. For more information about the limitations, see "Limitations".

You can configure fast restart in the **Parameter Estimator**, **Response Optimizer**, and **Sensitivity Analyzer** apps, or at the command line. For more information see, "Improving Optimization Performance Using Fast Restart (GUI)", "Improving Optimization Performance Using Fast Restart (Code)", "Use Fast Restart Mode During Response Optimization", or "Use Fast Restart Mode During Sensitivity Analysis".

Speed Up Using Accelerator Mode

Simulink Design Optimization software supports Normal and Accelerator simulation modes. You can accelerate the design optimization computations by changing the simulation mode of your Simulink model to Accelerator. For information about these modes, see "How Acceleration Modes Work".

The default simulation mode is **Normal**. In this mode, Simulink uses interpreted code, rather than compiled C code during simulations.

In the Accelerator mode, Simulink Design Optimization software runs simulations during optimization with compiled C code. Using compiled C code speeds up the simulations and reduces the time to optimize the model response signals.

For information about the limitations, and how to use the Accelerator mode, see "Use Accelerator Mode During Simulations".

See Also

Related Examples

- "Optimizing Time-Domain Response of Simulink Models Using Parallel Computing"
- "Improving Optimization Performance Using Fast Restart (GUI)"
- "Improving Optimization Performance Using Fast Restart (Code)"

Required and Related Products

Simulink Design Optimization software requires MATLAB, Simulink, and Optimization Toolbox $\ensuremath{^{\text{\tiny M}}}$ software.

The following table summarizes MathWorks[®] products that extend and complement the Simulink Design Optimization software. For current information about these and other MathWorks products, visit https://www.mathworks.com/products/.

Product	Description
Control System Toolbox	Enables you to design controllers for linear time- invariant (LTI) models using optimization methods.
Global Optimization Toolbox	Provides genetic algorithms, and direct search methods to estimate and optimize model parameters.
Deep Learning Toolbox	Provides Simulink models of neural networks for optimization-based control design.
Parallel Computing Toolbox	Enables parallel computing on multicore processors and multiprocessor networks to speed up estimation and optimization.
Simulink Control Design	Lets you linearize Simulink models. Use Simulink Design Optimization software to design controllers for linearized models using optimization methods.
Statistics and Machine Learning Toolbox	Provides additional probability distributions and statistical analysis techniques for sensitivity analysis.
System Identification Toolbox	Lets you estimate linear and nonlinear models from measured data. Import the estimated model into Simulink software, and use Simulink Design Optimization software for optimization-based control design.

- "Supported Data" on page 2-2
- "Prepare Data for Parameter Estimation" on page 2-3
- "Estimate Parameters from Measured Data" on page 2-11

Supported Data

From signal data, you can estimate model parameters and initial conditions of single or multiple input and output Simulink models.

Simulink Design Optimization software lets you estimate model parameters from the following types of data:

- *Time-domain* data Data with one or more input variables u(t) and one or more output variables y(t), sampled as a function of time. See "Import Data for Parameter Estimation".
- Time-series data Data stored in time-series objects. See "Time-Series Data".

Simulink Design Optimization software estimates model parameters by comparing the measured signal data with simulation data generated from the Simulink model. Using optimization techniques, the software estimates the parameters and initial conditions of states to minimize a user-selected cost function. The cost function typically calculates a least-square error between the measured and simulated data. To learn more, see "Estimate Parameters from Measured Data" on page 2-11.

See Also

More About

- "Time Series Objects and Collections"
- "Complex Data"

Prepare Data for Parameter Estimation

About This Tutorial

Objectives

This tutorial explains how to import, analyze, and prepare measured input and output (I/O) data for estimating parameters of a Simulink model.

Note Simulink Design Optimization software estimates parameters from real, time-domain data only.

Perform the following tasks using the **Parameter Estimator**:

- Import data from the MATLAB workspace.
- Analyze data quality using a time plot.
- Select a subset of data for estimation.
- Replace outliers.
- Filter high-frequency noise.

About the Sample Data

Load spe_engine_throttle1.mat, which contains I/O data measured from an engine throttle system. The MAT-file includes the following variables:

- input1 Input data samples
- position1 Output data samples
- time1 Time vector

Note The number of input and output data samples must be equal to the length of the corresponding time vector.

The engine throttle system controls the flow of air and fuel mixture to the engine cylinders. The throttle body contains a butterfly valve which opens when a driver presses the accelerator pedal. Opening this valve increases the amount of fuel mixture entering the cylinders, which increases the engine speed. A DC motor controls the opening angle of the butterfly valve in the throttle system. The input to the throttle system is the motor current (in amperes), and the output is the angular position of the butterfly valve (in degrees).

spe_engine_throttle1 contains the Simulink model of the engine throttle system.

Start a Parameter Estimator Session

To perform parameter estimation, you must first start a **Parameter Estimator** session.

1 Open the engine throttle system model by typing the following at the MATLAB prompt:

spe_engine_throttle1

This command opens the Simulink model, and loads the data into the MATLAB workspace.

1 U T Input U T Motor Throttle Throttle

Engine Throttle Model

2 In the Simulink model window, on the **Apps** tab, under **Control Systems**, select **Parameter Estimator**.

This action opens a new session, **Parameter Estimation - spe_engine_throttle1**, in the **Parameter Estimator**.

📣 Parame	ter Estimatior	n - spe_engin	e_throttle1						
PARA	METER ESTIMA	ATION	VALIDATI	ON	VIEW	<u>A</u> L		X B L b t b c	▲ ? ◄
								Cost Function: Sum Squared Error 💌	
Open Session 💌	Save Session 💌	New Experiment	Select Experiments	Select Parameters	Sensitivity Analysis ▼	Add Plot	Plot Model Response	Ø More Options	Estimate •
	LE	EXPERI	MENTS	PARAM	IETERS	PL	.OTS	OPTIONS	ESTIMATE
Data Brow	ser								
▼ Parame	ters								
			1						
Experim	ents		Ī						
- coperin			1						
			-						
 Results 									
 Preview 									
			1						
<u> </u>			1						

Note The Simulink model must remain open to perform parameter estimation tasks.

Create an Experiment for Parameter Estimation

In the **Parameter Estimator** on the **Parameter Estimation** tab, click the **New Experiment** button. This will create an experiment with the name Exp in the **Experiments** list on the left pane. You can rename it by right-clicking and selecting **Rename** from the list. For example, call it NewData1.

Import Data

This portion of the tutorial explains how to import measured I/O data into the experiment in the **Parameter Estimator**. Importing data assigns the data to the corresponding model input and output signals.

The model input and output signals are designated with the Inport Input and Outport Position blocks, respectively. To learn more about the blocks, see the Inport and Outport block reference pages in the Simulink documentation.

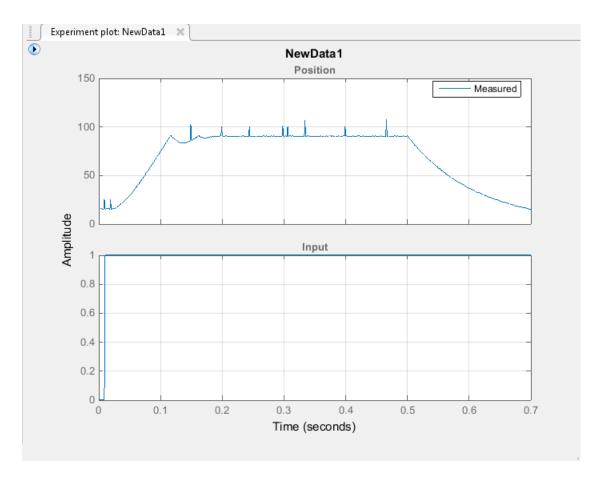
To import data into the experiment, right-click and select **Edit...** to launch the experiment editor. Import the output data by typing [time1,position1] in the dialog box in the **Outputs** panel. Import the input data by typing [time1,input1] in the dialog box in the **Inputs** panel.

Edit Experiment: NewData1	×
Outputs Define measured output signals for this experiment. spe engine throttle1/Throttle:1 (Position) <1x1 Signal, 701 points> <1x1 Signal, 701 points> Select Measured Output Signals	
Inputs Optionally define input signals for this experiment. spe engine throttle1/Input:1 (Input) [time1,input1] Select Inputs	=

Analyze Data

This portion of the tutorial explains how to analyze the output data quality by viewing the data characteristics on a time plot. Based on the analysis, you can decide whether to preprocess the data before estimating parameters. For example, if the data contains noise, you might want to filter the noise from the system dynamics before estimating parameters.

To create an experiment plot, click **Add Plot** on the **Parameter Estimation** tab and select the experiment name, for example, NewData1 under **Experiment Plots**.



The time plot shows the output data in response to a step input, as described in "About the Sample Data" on page 2-3. The plot shows a rapid decrease in the response after t = 0.5 s because the system is shut down. To focus parameter estimation on the time period when the system is active, select the data samples between t = 0 s and t = 0.5 s, as in "Extract Data for Estimation" on page 2-6.

The spikes in the data indicate *outliers*, defined as data values that deviate from the mean by more than three standard deviations. They might be caused by measurement errors or sensor problems. The response also contains noise. Before estimating model parameters from this data, remove the outliers and filter the noise, as described in "Replacing Outliers" on page 2-7 and "Filtering Data" on page 2-8.

You can also plot the experiment data by right-clicking the experiment, for example NewData1, and selecting **Plot measured experiment data** from the list.

Extract Data for Estimation

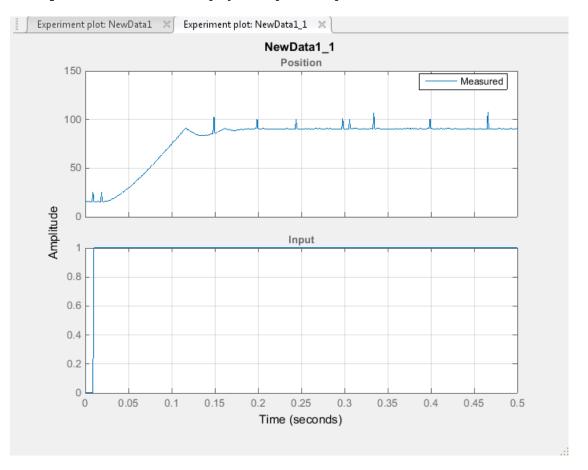
This portion of the tutorial explains how to select a subset of I/O data for estimation. As described in "Analyze Data" on page 2-5, the system is shut down at t = 0.5 s. To focus the estimation on the time period before t = 0.5 s, exclude the data samples beyond t = 0.5 s. This operation selects the data between t = 0 s and t = 0.5 s for estimation.

First, import the data into the experiment, as described in "Import Data" on page 2-5.

To select the portion of data between t = 0 s and t = 0.5 s:

- 1 Plot the measured data as described in "Analyze Data" on page 2-5, to have access to the **Experiment Plot** tab.
- 2 On the **Experiment Plot** tab, click **Extract Data** to launch the **Extract Data** tab.
- 3 Enter 0 in the **Start Time:** field and 0.5 in the **End Time:** field.
- 4 Click **Save As** to save data in a new experiment, for example, NewData1_1.

The **Parameter Estimator** extracts the corresponding input data. To plot the new data, click on **Add Plot** on the **Parameter Estimation** tab. Select the experiment name, for example, NewData1_1 in the **Experiment Plots** list to display the experiment plot of the data from t = 0 s to t = 0.5 s.



Replacing Outliers

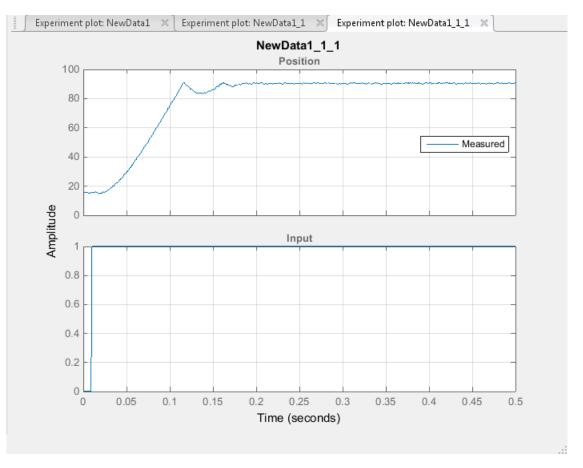
Why Replace Outliers

Outliers are data values that deviate from the mean by more than three standard deviations. When estimating parameters from data containing outliers, the results might not be accurate. Hence, you might choose to replace the outliers in the data before you estimate the parameters.

How to Replace Outliers

In the experiment plot of the data extracted as in "Extract Data for Estimation" on page 2-6, you can visually detect the data points that seem to be outliers. To replace these points:

- 1 In the **Experiment Plot** tab, click **Replace data** to launch the **Replace data** tab. The experiment plot shows the preview data, which is in light brown. On the preview, select the data point that you want to replace.
- 2 On the **Replace Data** tab, click **Replace data** and select the constant value. For example, replace the output signal data that correspond to time points 0.00899 and 0.0189 with 15, that corresponds to the time point 0.149 with 86, and the rest of the outlier data points with 90.
- 3 Click the arrow in the **Apply** section and select **Save As: Create a new experiment from the modified data**. **Parameter Estimator** saves the modified data in the new experiment, for example, NewData1_1_1.
- 4 Click Add Plot on the Parameter Estimation tab and select the new experiment, for example, NewData1_1_1. This creates an experiment plot of the modified data. The spikes, that indicated outliers, no longer appear on the time plot.



Filtering Data

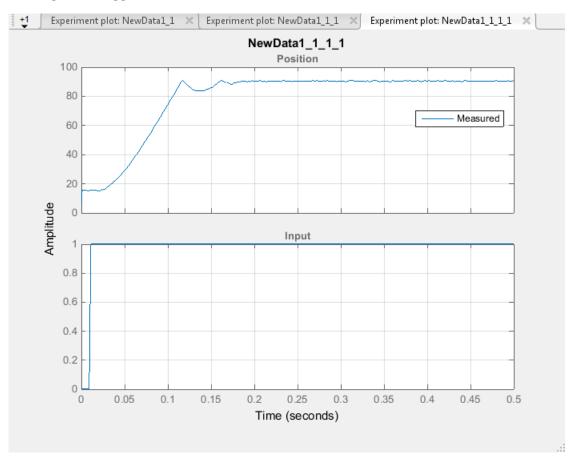
This portion of the tutorial explains how to filter the noise and remove any periodic trends from the output data. First remove the outliers from the output data, as described in "Replacing Outliers" on page 2-7.

Click the experiment plot for the new experiment, for example, NewData1_1_1. On the Experiment Plot tab, click Low-Pass Filter.

- 1 On the Low-Pass Filter tab select Filter all signals.
- 2 Enter 0.4 in the Normalized cutoff frequency field.
- 3 Click **Options**. Enter 1 in the **Filter order** field and click **OK**.

Filter Options			X
Filter order: Zero-pha		ift filter	
	ок	Cancel	Help

- 4 Click the arrow in the **Apply** section and select **Save As: Create a new experiment from the modified data**. **Parameter Estimator** saves the modified data in the new experiment, for example, NewData1_1_1_1.
- 5 Click Add Plot on the Parameter Estimation tab and select the new experiment, NewData1_1_1_1. This creates an experiment plot of the modified data. The noise is filtered and the output data appears smooth.



Saving the Session

After you prepare the data, delete the data in the older experiments, for example, New Data1, New Data1_1, New Data1_1_1. You can rename the last experiment, for example, NewData1_1_1_1 as NewData1, and save the session.

To delete the experiments, right-click the experiment name in the **Experiments** pane, and select **Delete** from the list.

To save the session, click **Save Session** on the **Parameter Estimation** tab to select where to save the session. Specify a name for the session, for example,

spe_engine_throttle1_sdosession.mat in the File name or Session field, and then click Save
or OK. This saves your parameter estimation session as a MAT-file.

To learn how to estimate parameters from this data, see "Estimate Parameters from Measured Data" on page 2-11.

Estimate Parameters from Measured Data

About This Tutorial

Objectives

This tutorial shows how to estimate parameters of a single-input single-output (SISO) Simulink model from measured input and output (I/O) data.

Note Simulink Design Optimization software estimates parameters from real, time-domain data only.

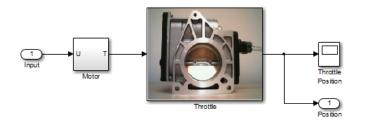
You can perform the following tasks using the **Parameter Estimator**:

- Load a saved session containing data
- Estimate model parameters using default settings
- Validate the model, and refine the estimation results

About the Model

This tutorial uses the **spe_engine_throttle1** Simulink model, which represents an engine throttle system.

Engine Throttle Model

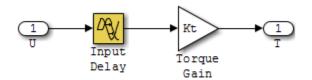


The throttle system controls the flow of air and fuel mixture to the engine cylinders. The throttle body contains a butterfly valve that opens when a driver presses the accelerator pedal. Opening this valve increases the amount of fuel mixture entering the cylinders, which increases the engine speed. A DC motor controls the opening angle of the butterfly valve in the throttle system. The models for these components are described in "Motor Subsystem" on page 2-11 and "Throttle Subsystem" on page 2-12.

The input to the throttle system is the motor current (in amperes), and the output is the angular position of the butterfly valve (in degrees).

Motor Subsystem

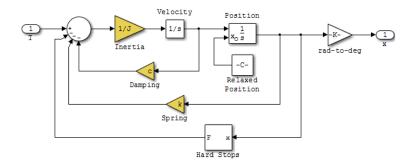
The Motor subsystem contains the DC motor model. To open the model, double-click the corresponding block.



Components of the Motor subsystem	Description
Variables	U is the input current to the motor.
	T is the torque applied by the motor.
Parameters	$K_{\rm t}$ is the torque gain of the motor, represented by Kt in the model.
	${\tt t}_d$ is the input time delay of the motor, represented by <code>input_delay</code> in the model.
Equation	The torque applied by the motor is described in the following equation:
	$T(t) = K_t U(t - t_d)$
	where t is time.
Input	U
Output	Т

Throttle Subsystem

The Throttle subsystem contains the butterfly valve model. To open the model, right-click the corresponding block, and select **Mask** > **Look Under Mask**.



The Hard Stops block models the valve angular position limit of 15° to 90°.

The following table describes the variables, parameters, states, differential equations, inputs, and outputs of the .

Components of the Throttle subsystem	Description			
Variables	T is the torque applied by the DC motor.			
	$\boldsymbol{\theta}$ is the angular position of the valve, represented by \mathbf{x} in the model.			
	$T_{hardstop}$ is the torque applied by the hard stop.			
Parameters	J is the valve inertia.			
	c is the valve viscous friction.			
	k is the valve spring constant.			
States	heta is the angular position.			
	$\dot{ heta}$ is the angular velocity.			
Equations	The mathematical system for the butterfly valve is described in the following equation:			
	$J\ddot{\theta} + c\dot{\theta} + k\theta = T + T_{hardstop}$			
	where $15^{\circ} \le \theta \le 90^{\circ}$, with initial conditions $\theta_0 = 15^{\circ}$,			
	and $\dot{\theta}_0 = 0$.			
	The torque applied by the Hard Stops block is described in the following equation:			
	$T_{hardstop} = \begin{cases} 0, & 15^{\circ} \le \theta \le 90^{\circ} \\ K(90^{\circ} - \theta), \theta > 90^{\circ} \\ K(15^{\circ} - \theta), \theta < 15^{\circ} \end{cases}$			
	where K is the gain of the Hard Stops block.			
Input	Т			
Output	θ			

Estimate Model Parameters Using Default Estimation Settings

Overview of the Estimation Process

Simulink Design Optimization software uses optimization techniques to estimate model parameters. In each optimization iteration, it simulates the model with the current parameter values. It computes and minimizes the error between the simulated and measured output. The estimation is complete when the optimization method finds a local minimum.

To start the estimation process, first open the engine throttle system Simulink model by typing the following at the MATLAB prompt:

spe_engine_throttle1

In the Simulink Toolstrip, on the Apps tab, under Control Systems, select Parameter Estimator.

This action opens a new session with the name **Parameter Estimation - spe_engine_throttle1** in the **Parameter Estimator**.

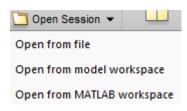
Note The Simulink model must remain open to perform parameter estimation tasks.

Specify Estimation Data and Parameters

1 Load or import the estimation data.

📣 Parameter Estimation	n* - spe_engii	ne_throttle1						
PARAMETER ESTIMATION		VALIDATION VIE		VIEW			A H & H to c	ē ? 🔺
				.			Cost Function: Sum Squared Error 👻	\triangleright
Open Save Session ▼ Session ▼	New Experiment	Select Experiments	Select Parameters	Sensitivity Analysis ▼	Add Plot	Plot Model Response	More Options	Estimate •
FILE	EXPERI		PARAM	ETERS	PL	LOTS	OPTIONS	ESTIMATE
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a If you prepared data and saved your session as described in "Prepare Data for Parameter Estimation" on page 2-3, load the preconfigured session. On the **Parameter Estimation** tab, click the **Open Session** drop down list.



Select the correct option to browse to the location of your saved session, for example, Open from file. Then select the MAT-file.

b If you do not have a previously saved session, create a new experiment. on the **Parameter Estimation** tab, click **New Experiment** . In the **Experiments** list on the left pane. You can

rename it by right-clicking and selecting **Rename** from the list. For example, call it NewData1.

To import data into the experiment, right-click and select **Edit...** to launch the experiment editor. Import the output data by typing in the dialog box in the **Outputs** panel, for example [time1, position1]. Import the input data by typing in the dialog box in the **Inputs** panel, for example [time1, input1].

Edit Experiment: NewData1	X
Outputs Define measured output signals for this experiment. spe engine throttle1/Throttle:1 (Position) <1x1 Signal, 701 points> Image: Select Measured Output Signals	
Inputs Optionally define input signals for this experiment. spe engine throttle1/Input:1 (Input) [time1,input1] Select Inputs	m

2 Specify parameters for estimation. On the Parameter Estimation tab, click the Select Parameters button to open the Edit: Estimated Parameters dialog box. In the Parameters Tuned for all Experiments panel, click the Select parameters button to launch the Select Model Variables dialog box.

Select the parameters J, c, input_delay, and k, and click OK.

Note In your application, if the model parameters you want to estimate are not listed in the Select Model Variables dialog box, first specify these parameters as variables. See, "Add Model Parameters as Variables for Estimation".

ilter by var	iable name		Q
•	Variable	Current value	Used By
1	J	0.05	<u>spe_engine_throttle1/Throttle</u>
	Kt	174.53	spe_engine_throttle1/Motor/TorqueGain
	angle_init	15	spe_engine_throttle1/Throttle
	angle_open	90	spe_engine_throttle1/Throttle
1	c	40	spe_engine_throttle1/Throttle
	input1	[0;0;0;0;0;0;0;0;0;0;0;:	
1	input_delay	0.02	spe_engine_throttle1/Motor/Input Delay_
V	k	1	<u>spe_engine_throttle1/Throttle</u>
	time1	[0;0.016638935108	
		ecessary (e.g., a(3) or s	·

Edit: Estimated Parameters		x
Parameters Tuned for all Experin	nents	
1		
• 0.05	-	🗶 🖾 Estimate
<u>c</u>		
40	▼ 🚽	🗙 🖾 Estimate
input delay		
• 0.02	- 4	🗙 🖾 Estimate
<u>k</u>		
1	▼ 🖶	🗶 🖾 Estimate
Belect parameters		
Parameters and Initial States Tun	ed per Experiment	t
There are no experiments selected fo		
Select Experiments	or estimation.	
Select Experimenta		
L		
	🔈 Update Model	🖋 OK (?) Help

The Edit: Estimated Parameters window now looks as follows.

The app selects the parameters you add for estimation by default. When estimating a large number of parameters, you can first select a subset of parameters to estimate.

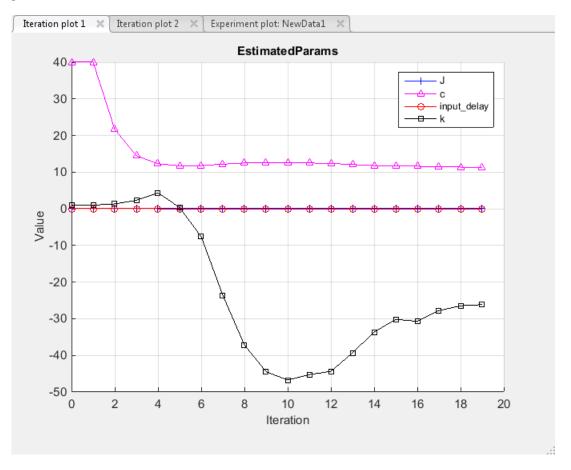
You can also first use sensitivity analysis to identify the parameters that most influence the estimation, and then specify these parameters for estimation. To open the **Sensitivity Analyzer**,

in the **Parameter Estimation** tab, click **Sensitivity Analysis**. In the **Sensitivity Analyze**, you can identify the model parameters that most influence the estimation problem and compute initial values for the estimation parameters.

3 Specify an experiment for estimation. On the **Parameter Estimation** tab, click **Select Experiments**, and select the box under the **Estimation** column. Click **OK**.

Select Experim	ents			×
Select experim	ents to includ	e for estimation or validation		
Estimation	Validation	Experiment		
7		NewData1		
				4
			🖌 ок	Help

- 4 To add progress plots, click Add Plot on the Parameter Estimation tab. Here you can choose the Parameter Trajectory and Estimation Cost iteration plots. You can also choose an experiment plot of measured and simulated data for NewData1.
- 5 Estimate the parameters using the default settings. On the Parameter Estimation tab, click Estimate to open the Parameter Trajectory plot and Estimation Progress Report window



and estimate the parameters. The **Parameter Trajectory** plot shows the change in the parameter values at each iteration.

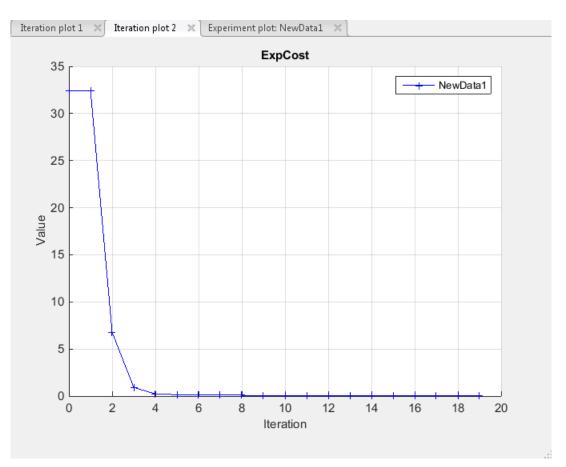
The **Estimation Progress Report** shows the iteration number, number of times the objective function is evaluated, and the value of the cost function at the end of each iteration. After the estimation converges, the **Estimation Progress Report** looks like this figure.

Iteration	F-count	NewData1	
		(Minimize)	
0	9		32.4446
1	18		32.4446
2	27		6.7733
3	36		0.9226
4	45		0.2299
5	54		0.1505
6	63		0.1272
7	72		0.0992
8	81		0.0858
9	90		0.0778
10	99		0.0702
11	108		0.0642
12	117		0.0591
13	126		0.0552
14	135		0.0534
15	144		0.0520
16	153		0.0508
17	162		0.0497
18	171		0.0486
19	180		0.0479
Ontimizatio	on started 16	-Jun-2014 16:19:52	
		18-Jun-2014 16:20:44	E
Estimated p	parameter v	updated with estimated parameter values alues written to 'EstimatedParams' values written to 'NewData1'	
	solver outpu		

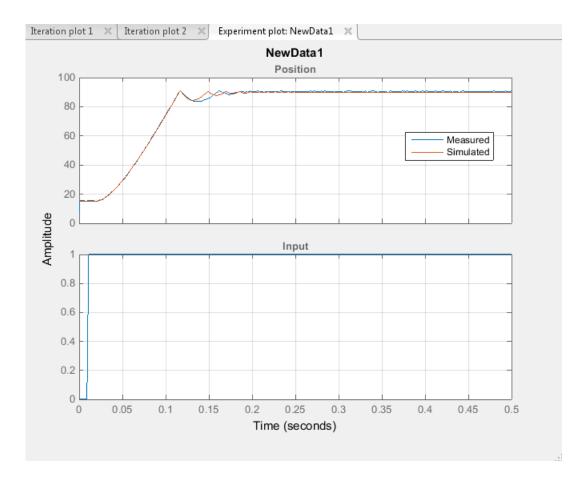
The estimated parameters are saved in the **Parameter Estimator**, in the **Results** section of the **Data Browser** pane, as EstimatedParams. Right-click EstimatedParams, and select **Open...** to view the results.

iew Result : EstimatedParams
Estimation result(s):
J = 0.22708
c = 11.346
input_delay = 0.0094873
k = -26.119
Parameters estimated using experiments:
NewData1, cost = 0.047861
Solver output:
Cost: 0.047861
ExitFlag: 3
FCount: 181
Date: 16-Jun-2014 16:20
Solver termination message:
Local minimum possible.
Isqnonlin stopped because the final change in the sum of squares relative to
its initial value is less than the selected value of the function tolerance.
Stopping criteria details:
Optimization stopped because the relative sum of squares (r) is changing by less than options.TolFun = 1.000000e-03.
Optimization Metric Options
relative change r = 6.65e-04 TolFun = 1e-03 (selected)
Η Use as initial guess 🛛 📓 Update Model 🛛 🛫 Of

6 Examine the estimated cost function graph. Cost function is the error between the simulated and measured output. During estimation, the default optimization method Nonlinear least squares, lsqnonlin, minimizes the cost function by changing the parameter values. The following figure displays the change in the expected cost during iterations.



7 Examine the simulated response plot to see how well the simulated output matches the measured output. The experiment plot shows that the output simulated using the estimated parameters is close to the measured outputs.



Improve Estimation Results Using Parameter Bounds

You can improve the accuracy of estimation by specifying bounds on parameter values. This technique restricts the region in which the optimization method searches for a local minima.

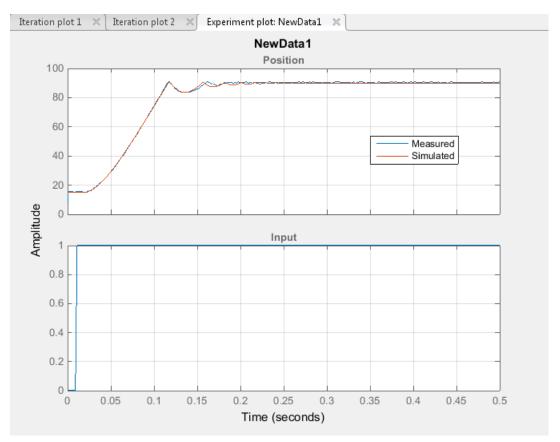
The engine throttle system has these characteristics:

- All parameter values are positive.
- Maximum time delay of the system, represented by input_delay, is 0.1 s.

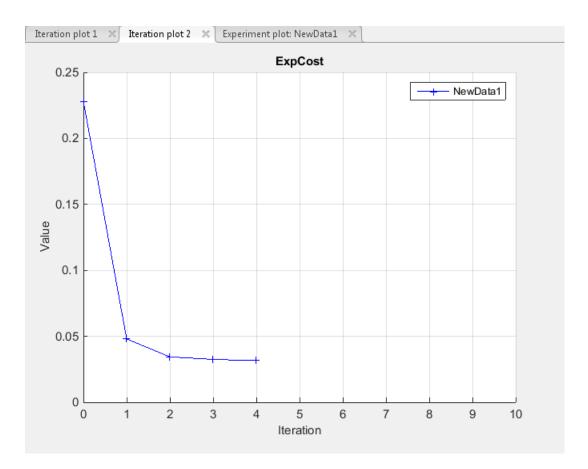
Therefore, specify 0 as the minimum value for all parameters, and 0.1 as the maximum value of input_delay. In the **Parameter Estimator**, click the **Select Parameters** button to specify bounds on the parameter values. For each parameter, click the right arrow toggle to display the minimum, maximum, and scale fields. Specify the minimum value for each parameter by replacing -Inf with 0 in the **Minimum** field. Specify the maximum value for input_delay by replacing +Inf with 0.1 in the corresponding **Maximum** field.

input dela	Ϋ́		
▼ 0.02		▼ 🖶	🗶 🗹 Estimate
Minimum:	0	▼ 🖶	
Maximum:	0.1	▼ 🖶	
Scale:	0.03125	▼ 🖶	

After estimating the parameters, analyze the results using the experiment plot and the plot for expected cost.



The data simulated using the estimated parameter values agree better with the measured data than when the parameter limits were not specified.



Validate Estimated Model Parameters

After estimating model parameters, validate the model using another data set (*validation data*). A good match between the simulated response and the validation data indicates that you have not overfitted the model.

To validate the estimated parameters using a validation data set:

Create a new experiment to use for validation. Name it ValidationData. Import the validation I/O data, input2 and position2, and the time vector, time2 in the ValidationData experiment. To do this, in the **Parameter Estimator**, in the Experiments pane, right-click ValidationData and select **Edit...** to open the experiment editor. Then, type [time2, position2] in the output dialog box and [time2, input2] in the input dialog box. For more information, see "Import Data for Parameter Estimation".

Edit Experiment: ValidationData	×
Outputs	
Specify measured output signals for this experiment.	
/Throttle:1 (Position)	
[time2,position2]	🗕 🗗 🕂 🔺
Select Measured Output Signals	

2 Select the experiment for validation. On the **Parameter Estimation** tab, click **Select Experiments**. By default, the ValidationData experiment is selected for estimation. Deselect the check box that corresponds to ValidationData for estimation and select the check box for validation.

Select Experime	ents			×
Select experim	ents to includ	le for estimation or validation		
Estimation	Validation	Experiment		
V		NewData1		
		ValidationData		Å
		🛩 ок	?	Help

3 Select results to use. On the Validation tab, click Select Results to Validate.

PARAMETER ESTIMATION			VALIDATION	EXPERIMENT PLOT
New Experiment	Select Experiments	Select Res to Valida	sults	d & Simulated Data
EXPERIMENTS		RESULT	rs PLOT O	PTIONS VALIDATE

Deselect Use current parameter values and select EstimatedParams, and click OK.

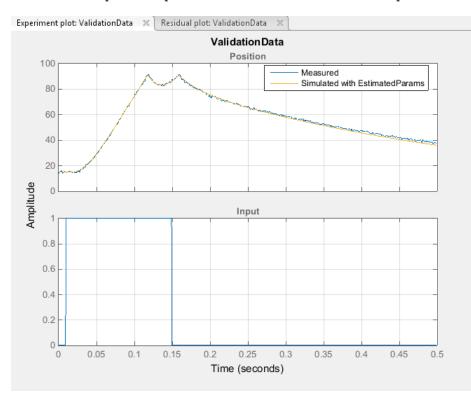
Select Re	sults	X
	Select estimation results to validate	
	Results	
	Use current parameter values	
V	EstimatedParams	
	Selected results are used to simulate the model and compare with measured exprin	nent data.
	🖋 ок	Help

4 Select the plots for measured and simulated data, and residuals on the **Validation** tab. You can assess how much the data simulated using the estimated parameters agrees with the measured data using these plots.

Plot Measured & Simulated Data
Plot Residuals

On the Validation tab, click Validate to start validation.

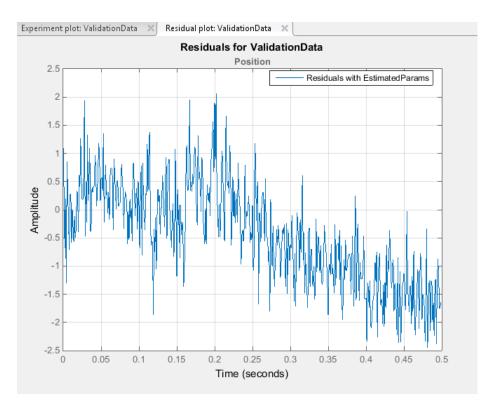
5 Examine the plots.



a Examine the experiment plot to see how well the simulated output matches the output data.

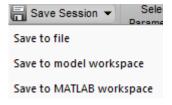
The simulated response as shown in light brown on the top experiment plot is overlaid on the measured out put data, and closely matches the measured validation data.

b Examine the residuals plot to compare the difference between the simulated response and measured data.



The difference between the simulated and measured data varies between 2 and -2.5. The residuals lie within 6% of the maximum output variation and do not display any systematic patterns. This indicates a good fit between the simulated output and measured data.

6 Save the session. On the **Parameter Estimation** tab, click **Save Session**.



From the drop-down list select where to save the session. Specify the file name, and click **Save** or **OK** to save your parameter estimation session as a MAT-file.

Response Optimization

- "Supported Design Requirements" on page 3-2
- "Design Optimization to Meet Step Response Requirements (GUI)" on page 3-3
- "Design Optimization to Meet Step Response Requirements (Code)" on page 3-14
- "Design Optimization to Track Reference Signal (GUI)" on page 3-20
- "Design Optimization Using Frequency-Domain Check Blocks (GUI)" on page 3-31
- "Time-Domain Model Verification" on page 3-39

Supported Design Requirements

You can optimize response of Simulink models to meet time-domain and frequency-domain design requirements.

Simulink Design Optimization software optimizes model response by formulating the requirements into a constrained optimization problem. It then solves the problem using optimization methods.

• For time-domain requirements, the software simulates the model during optimization, compares the current response with the requirement and uses gradient methods to modify design variables (model parameters) to meet the objectives.

You can specify time-domain requirements either in blocks from the **Signal Constraints** library or without adding blocks to the model. You can also include requirements specified in Check Static Range, Check Static Lower Bound and Check Static Upper Bound blocks from the Simulink **Model Verification** library.

• For frequency-domain requirements, the software linearizes the portion of the model between specified linearization inputs and outputs, compares the linear system with the requirement and uses gradient methods to modify the design variables to meet the objectives.

If you have Simulink Control Design software, you can optimize the model to meet frequencydomain requirements, such as Bode magnitude and gain and phase margin bounds. You can specify the frequency-domain requirements without adding blocks to the model or by using the "Model Verification" (Simulink Control Design) blocks of the Simulink Control Design software library.

Related Examples

"Design Optimization to Meet Step Response Requirements (GUI)" on page 3-3

"Design Optimization to Meet Step Response Requirements (Code)" on page 3-14

"Design Optimization to Track Reference Signal (GUI)" on page 3-20

"Design Optimization to Meet Frequency-Domain Requirements (GUI)"

"Design Optimization Using Frequency-Domain Check Blocks (GUI)" on page 3-31

Design Optimization to Meet Time- and Frequency-Domain Requirements (GUI)

More About

"How the Optimization Algorithm Formulates Minimization Problems"

"Specify Time-Domain Design Requirements in the App"

"Specify Frequency-Domain Design Requirements in the App"

Design Optimization to Meet Step Response Requirements (GUI)

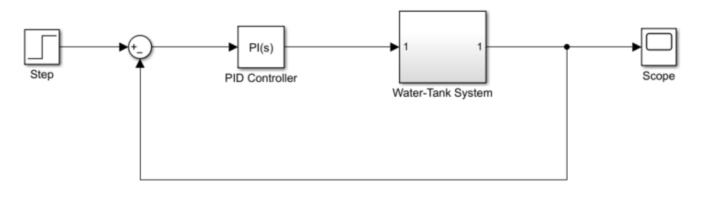
This example shows how to optimize controller parameters to meet step response design requirements using the **Response Optimizer** app. You specify the design requirements in a Check Step Response Characteristics block.

Model Structure

This example uses the watertank_stepinput model. This model includes the nonlinear Water-Tank System plant and a PI controller in a single-loop feedback system.

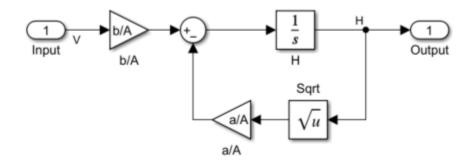
Open the model.

sys = 'watertank_stepinput';
open_system(sys)

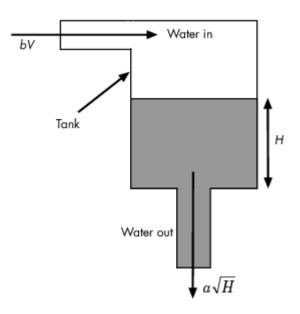


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To view the water tank model, open the Water-Tank System subsystem.



This model represents the following water tank system.



Here:

- Vol is the volume of water in the tank.
- *A* is the cross-sectional area of the tank.
- *H* is the height of water in the tank.
- *V* is the voltage applied to the pump.
- *b* is a constant related to the flow rate into the tank.
- *a* is a constant related to the flow rate out of the tank.

Water enters the tank at the top at a rate proportional to the valve opening. The valve opening is proportional to the voltage, V, applied to the pump. The water leaves through an opening in the tank base at a rate that is proportional to the square root of the water height, H. The presence of the square root in the water flow rate results in a nonlinear plant. Based on these flow rates, the rate of change of the tank volume is:

$$\frac{d}{\mathrm{d}t}Vol = A\frac{\mathrm{d}}{\mathrm{d}t}H = bV - a\sqrt{H}$$

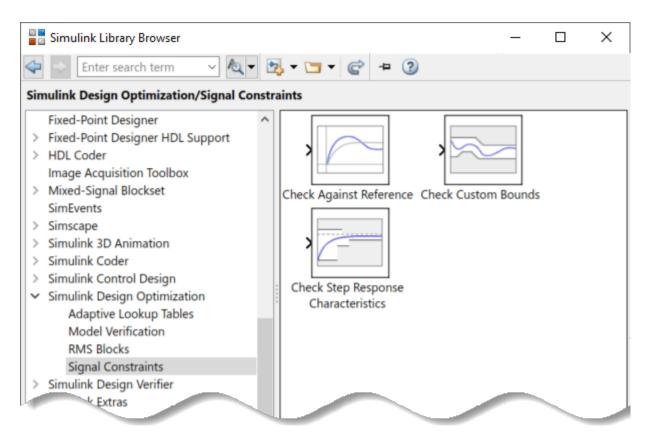
Design Requirements

The height of water in the tank, H, must meet the following step response requirements.

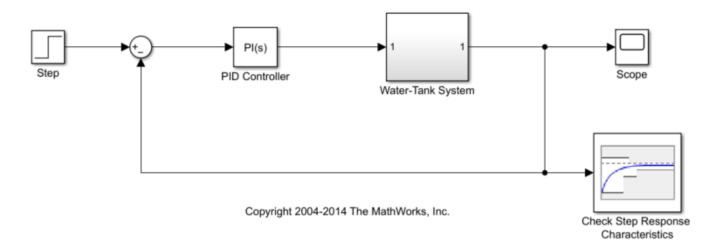
- Rise time less than 2.5 seconds
- Settling time less than 20 seconds
- Overshoot less than 5%

Specify Step Response Requirements

To specify step response requirements, add a Check Step Response Characteristics block to the model. To do so, in the Simulink® model window, on **Simulation** tab, click **Library Browser**. In the **Simulink Design Optimization** list, select **Signal Constraints**.



Drag and drop the Check Step Response Characteristics block into the model window and connect the block to the output. The block is connected to the signal for which you want to specify design requirements.



Double-click the Check Step Response Characteristics block to open the block parameters dialog and specify the following requirements:

• In Rise time (seconds), enter 2.5.

- In Settling time (seconds), enter 20.
- In % Overshoot, enter 5.
- In Initial value, enter 1.
- In Final value, enter 2.

눰 Block Parameters: Check S	Step Response Characte	ristics				×		
- Check Step Response Cha	racteristics							
Assert that the input signa	al satisfies bounds sp	ecifie	d by step i	respons	se characteris	tics.		
Bounds Assertion								
Dounds Assertion								
☑ Include step response	bound in assertion							
Step time (seconds):	0	:						
Initial value:	1	:	Final valu	e:	2	:		
Rise time (seconds):	2.5	:	% Rise:		80	:		
Settling time (seconds):	20	:	% Settling	g:	1	:		
% Overshoot:	5	:	% Unders	shoot:	1	:		
✓ Enable zero-crossing detection								
Show Plot Show plot	on block open				Response O	ptimization		
0		0	(C	ancel	Help	Apply		

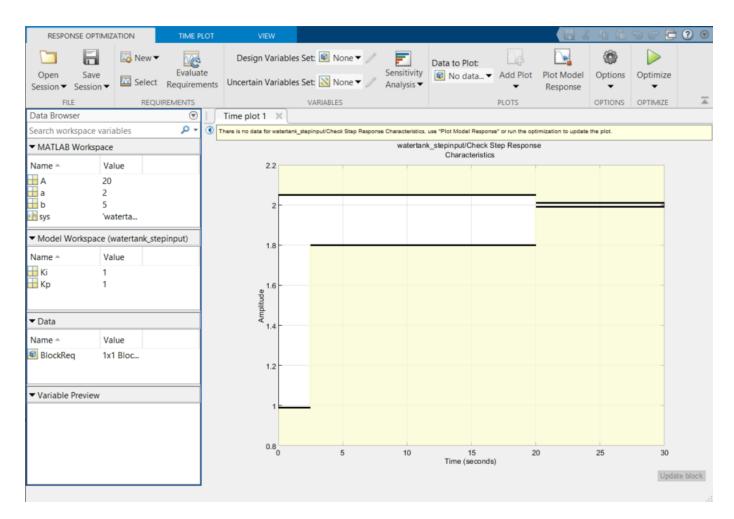
Click OK.

Instead of specifying time-domain requirements in the Check blocks, you can specify them in the **Response Optimizer** without adding blocks. For an example that uses this approach, see "Design Optimization to Track Reference Signal (GUI)" on page 3-20.

Specify Design Variables

When you optimize the model response, the software modifies the design variable values to meet the design requirements. You specify which model parameters the software can modify.

To open a **Response Optimizer** session for this model, in the Simulink model window, in the **Apps** gallery, click **Response Optimizer**. Alternatively, in the Check Step Response Characteristics block parameters dialog, click **Response Optimization**.



The region bounded by black line segments in **Time plot 1** shows the step response requirements that you specified in the Check Step Response Characteristics block.

To create a set of design variables, in the **Design Variables Set** list, select New.

RESPO	RESPONSE OPTIMIZATION TIME PLOT			VIEW							
		🔯 New 🔻		Design Variables	Set:	😰 None 🔻 🥖	F	Data to Plot	1		
Open Session 🔻	Save Session▼	Select	Evaluate Requirements	Uncertain Variables	Set:	CREATE NEW SET	OF DESIG	N VARIABLES		Add Plot	Plot Moo Respon
FIL	E	REQU	JIREMENTS		VA	New Use to specify	v variables	used	F	PLOTS	
Data Brows	ser			Time plot 1 🛛 🕅		by the Simulir					
Search wor	kspace varia	ables	ρ - 💽	There is no data for watertank_	stepinp	ut/Check Step Response C	Characteristics,	use "Plot Model Res	ponse"	or run the opti	mization

The Create Design Variables Set dialog box shows model parameters that you can use as design variables and indicates their locations within the model.

C	reate Design Variables	Set							×		
(reate Design Variable	s set: De	signVars								
	Variable	Value	Minim	Maxim	Scale		Variable	Current va	Used By		
						-	А	20	watertank stepinput/Water-Tank System/a//A,		
						4	Ki	1	watertank stepinput/PID Controller		
	Add model variables to optimize.			Кр	1		watertank stepinput/PID Controller				
						Ū	а	2	watertank stepinput/Water-Tank System/a//A		
							b	5	watertank stepinput/Water-Tank System/b//A		
			Update	model va	ariables						
	Variable Detail			-	Specify ex	pression ind	lexing if necessary (e.g., a(3) or s.x)				
	- Vanabic Detail								OK Cancel Help		

To add parameters to the design variable set, select Ki and Kp, and click

	Design Variables Design Variables		signVars		
	Variable	Value	Minim	Maxim	Scale
\checkmark	Ki	1	-Inf	Inf	1
\checkmark	Кр	1	-Inf	Inf	1

The design variables list displays the following variable settings:

- Variable Variable name
- Value Current variable value
- Minimum and Maximum Variable bounds
- **Scale** Scaling factor for the variable

Limit the design variables to positive values. To do so, enter 0 for the minimum value of each variable in the corresponding **Minimum** field and press Enter on your keyboard.

eate Design Variable	s Set es set: De	signVars						
Variable	Value	Minim	Maxim	Scale	1	Variable	Current va	Used By
🗹 Ki	1	0	Inf	1		A	20	watertank stepinput/Water-Tank System/a//A,
🗹 Кр	1	0	Inf	1		a	2	watertank stepinput/Water-Tank System/a//A
					4	b	5	watertank stepinput/Water-Tank System/b//A
					đ			·
		Update	model va	riables	1			
Variable Detail						Specify ex	pression ind	lexing if necessary (e.g., a(3) or s.x)
								OK Cancel Hel

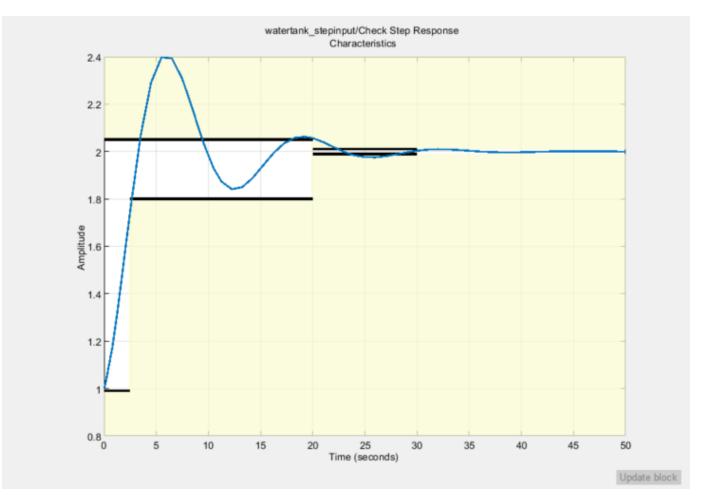
Click **OK**. A new design variable **DesignVars** is created and appears in the **Data** area of **Response Optimizer**. You can click the variable to view its contents in the **Variable Preview** area.

▼ Model Workspace	ce (watertan	k_stepinput)
Name 🔶	Value	
🔠 Ki	1	
🗄 Кр	1	
▼ Data		
Name 🔶	Value	
BlockReq	1x1 Bloc	
DesignVars	2x1 Cont	
▼ Variable Preview	1	
<pre>DesignVars(1,1) =</pre>		^
Name: 'Ki'		
Value: 1		
Minimum: 0 Maximum: Inf		
Free: 1		~

If your model has many parameters, you can first use sensitivity analysis to determine the most influential parameters to optimize, or to obtain initial guesses for the design variables. For more information, see "What is Sensitivity Analysis?" Using the **Sensitivity Analyzer** app, you can explore the response optimization design space by altering the design variables, identify the parameters that most influence the optimization problem, and compute initial values.

Optimize Model Response

To view the current response of the model, click **Plot Model Response**.



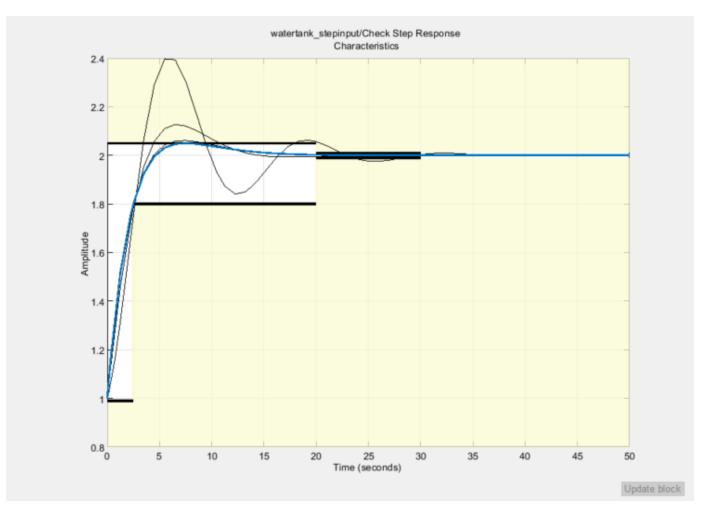
The plot shows the model output, depicted by the blue line, lies outside the region of the specified step response.

To optimize the model response, click **Optimize**. The default optimization solver **Gradient descent** (fmincon) modifies the design variables at each iteration so that the simulated response lies within the design requirement line segments. For more information, see "How the Optimization Algorithm Formulates Minimization Problems".

Iteration	F-count	Check Step Response Characteristics (Upper)		
		(<=0)		
0	5		(0.801
1	10		(0.037
2	15		(0.005
3	20		9,144	46e-(
4	25		2.568	88e-(
ptimization starte	d 22-Nov-2021 1	40.47		_
				- 1
ptimization conve	arged, 22-Nov-20	110:41:13		
ptimized variable atertank_stepinpu		"DesignVars' in the Design Optimization workspace		
		n to 'ReqValues' in the Design Optimization workspace		

The message Optimization converged in the Optimization Progress Report indicates that the optimization solver found a solution that meets the design requirements within the tolerances and parameter bounds. For more information about the outputs displayed in the optimization, see "Iterative Display".

Verify that the model output meets the step response requirements.



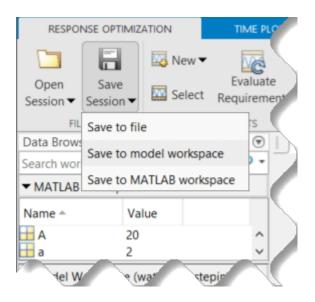
The plot displays the last five iterations. The final response using the optimized variable parameter appears as the thick blue line. The optimized response lies in the white region bounded by the design requirement line segments and thus meets the requirements.

To view the optimized parameter values, click DesignVars in Model Workspace and view the updated values in the Variable Preview area. The optimized values of the design variables are automatically updated in the Simulink model.

Save the Session

After you optimize the model response to meet design requirements, you can save the **Response Optimizer** session which includes the optimized parameter values.

In the **Response Optimizer**, in the **Response Optimization** tab, in the **Save Session** drop-down list, select **Save to model workspace**.



In the Save Session window, specify the session name in the **Session** field.

To open the saved session, in the **Response Optimizer** for the model, in the **Open Session** dropdown list, click the **Open from model workspace** option.

Close the model.

bdclose('all')

See Also

Related Examples

- "Design Optimization to Meet Step Response Requirements (Code)" on page 3-14
- "Design Optimization to Track Reference Signal (GUI)" on page 3-20

Design Optimization to Meet Step Response Requirements (Code)

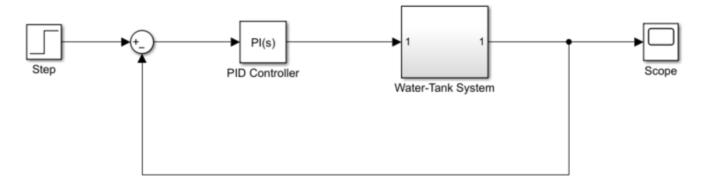
This example shows how to programmatically optimize controller parameters to meet step response requirements using the sdo.optimize function.

Model Structure

This example uses the watertank_stepinput model. This model includes the nonlinear Water-Tank System plant and a PI controller in a single-loop feedback system.

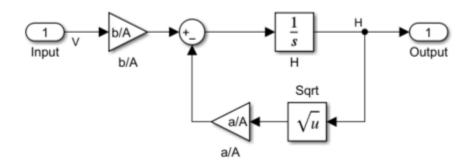
Open the model.

```
sys = 'watertank_stepinput';
open_system(sys)
```

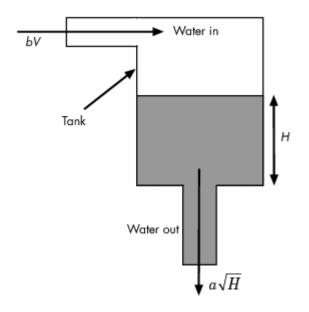


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To view the water tank model, open the Water-Tank System subsystem.



This model represents the following water tank system.



Here:

- *Vol* is the volume of water in the tank.
- *A* is the cross-sectional area of the tank.
- *H* is the height of water in the tank.
- *V* is the voltage applied to the pump.
- *b* is a constant related to the flow rate into the tank.
- *a* is a constant related to the flow rate out of the tank.

Water enters the tank at the top at a rate proportional to the valve opening. The valve opening is proportional to the voltage, V, applied to the pump. The water leaves through an opening in the tank base at a rate that is proportional to the square root of the water height, H. The presence of the square root in the water flow rate results in a nonlinear plant. Based on these flow rates, the rate of change of the tank volume is:

$$\frac{d}{dt}Vol = A\frac{d}{dt}H = bV - a\sqrt{H}$$

Design Requirements

The height of water in the tank, H, must meet the following step response requirements:

- Rise time less than 2.5 seconds
- Settling time less than 20 seconds
- Overshoot less than 5%

Specify Step Response Requirements

During optimization, the model is simulated using the current value of the model parameters and the logged signal is used to evaluate the design requirements.

For this model, log the water level, H.

```
PlantOutput = Simulink.SimulationData.SignalLoggingInfo;
PlantOutput.BlockPath = [sys '/Water-Tank System'];
PlantOutput.OutputPortIndex = 1;
PlantOutput.LoggingInfo.NameMode = 1;
PlantOutput.LoggingInfo.LoggingName = 'PlantOutput';
```

Next, create a **sdo.SimulationTest** object to store the logging information. You also use this later to simulate the model.

```
simulator = sdo.SimulationTest(sys);
simulator.LoggingInfo.Signals = PlantOutput;
```

Specify the step response requirements.

```
StepResp = sdo.requirements.StepResponseEnvelope;
StepResp.RiseTime = 2.5;
StepResp.SettlingTime = 20;
StepResp.PercentOvershoot = 5;
StepResp.FinalValue = 2;
StepResp.InitialValue = 1;
```

StepResp is a sdo.requirements.StepResponseEnvelope object. The values assigned to
StepResp.FinalValue and StepResp.InitialValue correspond to a step change in the water
tank height from 1 to 2.

Specify Design Variables

When you optimize the model response, the software modifies parameter (design variable) values to meet the design requirements.

Select model parameters to optimize. Here, optimize the parameters of the PID controller.

```
p = sdo.getParameterFromModel(sys,{'Kp','Ki'});
```

p is an array of two param.Continuous objects.

To limit the parameters to positive values, set the minimum value of each parameter to 0.

```
p(1).Minimum = 0;
p(2).Minimum = 0;
```

Optimize Model Response

Create a design function to evaluate the system performance for a set of parameter values.

```
evalDesign = @(p) sldo_model1_design(p,simulator,StepResp);
```

evalDesign is an anonymous function that calls the cost function sldo_model1_design. The cost function simulates the model and evaluates the design requirements. To view this function, type edit sldo_model1_design at command line.

Compute the initial model response using the current values of the design variables.

```
initDesign = evalDesign(p);
```

Examine the nonlinear inequality constraints.

initDesign.Cleq

ans = 8×1 0.1739 0.0169 -0.0002 -0.0101 -0.0229 0.0073 -0.0031 0.0423

Some Cleq values are positive, beyond the specified tolerance, which indicates the response using the current parameter values violate the design requirements.

Specify optimization options.

opt = sdo.OptimizeOptions; opt.MethodOptions.Algorithm = 'sqp';

The software configures **opt** to use the default optimization method, fmincon, and the sequential quadratic programming algorithm for fmincon.

Optimize the response.

```
[pOpt,optInfo] = sdo.optimize(evalDesign,p,opt);
```

Optimization started 01-Sep-2022 13:38:52

				max			First-order
Iter	F-count		f(x)) constra	aint	Step-size	optimality
Θ	5		0	0.1	1739		
1	10		0	0.0	3411	1	0.81
2	15		0	Ð	0	0.235	0.0429
3	15		0	•	0	2.71e-19	Θ
Local	minimum	found	that	satisfies	the	constraints.	

Optimization completed because the objective function is non-decreasing in feasible directions, to within the value of the optimality tolerance, and constraints are satisfied to within the value of the constraint tolerance.

At each optimization iteration, the software simulates the model and the default optimization solver fmincon modifies the design variables to meet the design requirements. For more information, see "How the Optimization Algorithm Formulates Minimization Problems".

The message Local minimum found that satisfies the constraints indicates that the optimization solver found a solution that meets the design requirements within specified tolerances. For more information about the outputs displayed during the optimization, see "Iterative Display".

Examine the optimization termination information contained in the optInfo output argument. This information helps you verify that the response meets the step response requirements.

For example, check the Cleq and exitflag fields.

Cleq shows the optimized nonlinear inequality constraints.

optInfo.Cleq

ans = 8×1

-0.0001 -0.0028 -0.0050 -0.0101 -0.0135 -0.0050 -0.0050 -0.0732

All values satisfy $Cleq \leq 0$ within the optimization tolerances, which indicates that the step response requirements are satisfied.

exitflag identifies why the optimization terminated.

optInfo.exitflag

ans = 1

The value is 1, which indicates that the solver found a solution that was less than the specified tolerances on the function value and constraint violations.

View the optimized parameter values.

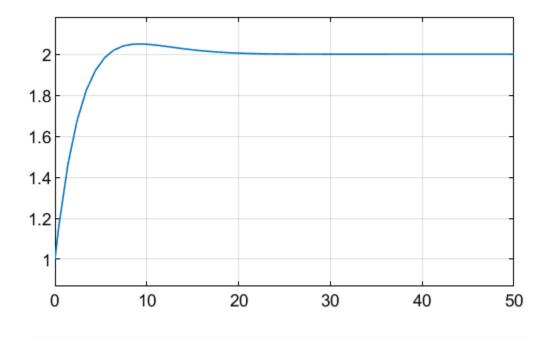
p0pt

```
pOpt(1,1) =
      Name: 'Kp'
     Value: 2.0545
   Minimum: 0
   Maximum: Inf
      Free: 1
     Scale: 1
      Info: [1x1 struct]
pOpt(2,1) =
      Name: 'Ki'
     Value: 0.3801
   Minimum: 0
   Maximum: Inf
      Free: 1
     Scale: 1
      Info: [1x1 struct]
```

2x1 param.Continuous

Simulate the model with the optimized values.

```
sdo.setValueInModel(sys,pOpt);
sim(sys);
```



Verify that the model output meets the step response requirements.

Close the model.

close_system(sys,0);

See Also

sdo.optimize|Simulink.SimulationData.SignalLoggingInfo|sdo.SimulationTest| sdo.getParameterFromModel|sdo.requirements.StepResponseEnvelope| param.Continuous|sdo.OptimizeOptions

Related Examples

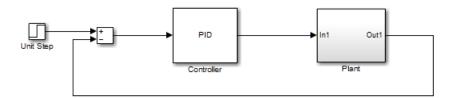
- "Design Optimization to Meet Step Response Requirements (GUI)" on page 3-3
- "Design Optimization to Track Reference Signal (GUI)" on page 3-20
- "Discrete-Valued Variables in Response Optimization (Code)"

Design Optimization to Track Reference Signal (GUI)

This example shows how to optimize controller parameters to track a reference signal using the **Response Optimizer**. You specify the reference signal without adding any Check blocks to the model.

Model Structure

The model sldo_model1 includes these blocks:



- Controller block, a PID controller, controls the output of the Plant subsystem.
- Unit Step block applies a step input.

You can also use other types of inputs, such as ramp, to optimize the response generated by such inputs.

• Plant subsystem is a second-order system with delay. It contains Transfer Function and Transport Delay blocks.



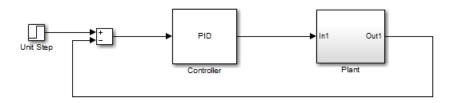
Design Requirements

The model output must track a reference signal $y = 1 - \exp(-0.1 \times t)$, where *t* is time.

Specify Reference Signal

1 Open the Simulink model.

```
sys = 'sldo_model1';
open_system(sys);
```

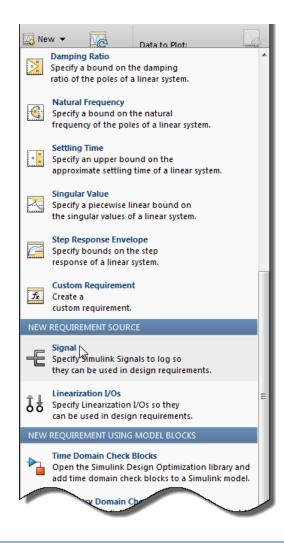


To learn more about the model, see "Model Structure" on page 3-20.

2 To open the **Response Optimizer**, in the Simulink model window, from the **Apps** tab, in the gallery, under **Control Systems**, select **Response Optimizer**.

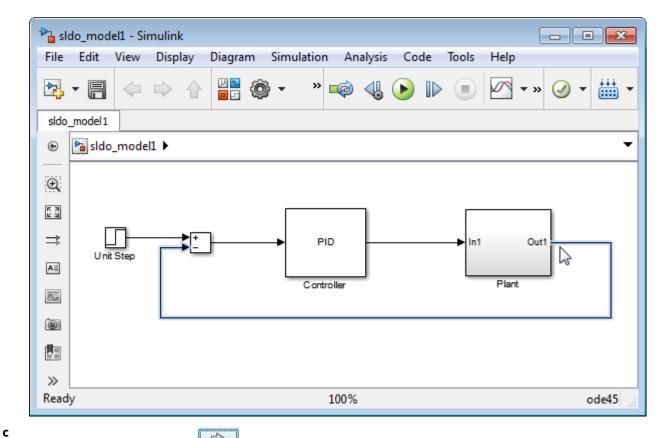
RESPONSE OPT		VIEW			SH1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-			: ?
	New 👻		Design Variables Set: 😰 None 👻 🖉	.	Data to Plot:			
Open Save Session - Session		Evaluate Requirements	uncertain Variables Set: 📉 None 👻 🚄	Sensitivity Analysis 💌	No data selected Add Plot	Plot Model Response	Options Optimiz	e
FILE	REQU	IREMENTS	VARIABLES		PLOTS		OPTIONS OPTIMIZ	E
Data Browser								
Search workspace v	ariables	- ۹						
 MATLAB Worksp 	ace							
Name 🔺	Value							
abc sys	'sldo_mod.							
	-							
 Model Workspace 	e (sldo_model1)							
Name 🔺	Value							
- Kd	0							
🕂 Ki	0	E						
Н Кр н w0	1 0.5000	+						
▼ Data	0.5000							
Name 📥	Value							
 Variable Preview 								

- **3** Select the model signal to track the reference signal.
 - a In the New drop-down list, select Signal to open the Create Signal Set window.



Create Signal Set			×
Signal set: Sig			
		Signal	
No signals have currently been selected. Please go back to the model and click on a signal to select it.	•		1
		OK Cancel	Help

b To display the signal in the window, click the output of the Plant block in the Simulink model window.



Select the signal, and click to add it to the signal set.

Create Signal Set			×
Signal set: Sig			
Currently selected signals]	Signal	
sldo_model1/Plant : 1		sldo_model1/Plant:1	
			1
	2		
		OK Cancel	Help

d In **Signal set**, enter **PlantOutput** as the selected signal name.

Click **OK** to create the variable **PlantOutput**. It appears in the **Data** area of the **Response Optimizer**.

- 4 Specify the reference signal for the model output to track.
 - a In the New drop-down list, select Signal Tracking to open a Create Requirement window.
 - **b** In the **Name** edit box, enter ref_sig.
 - c In the **Time vector** edit box, enter linspace(0,50,200)
 - d In the Amplitude edit box, enter 1-exp(-0.1*linspace(0,50,200)).

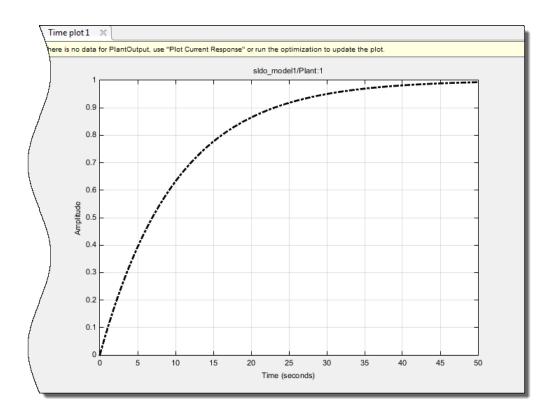
Create Requirement		х
	Signal Tracking	
	Specify a tracking requirement on a signal.	
Name: ref_sig		
 Specify Reference 	nce Signal	
Time vector:	linspace(0,50,200)	
Amplitude:	1-exp(-0.1*linspace(0,50,200))	
	Update reference signal data]
Tracking Method:	SSE 🔻	

Leave the **Tracking Method** as SSE which means, at each optimization iteration, the solver attempts to reduce the sum of squared errors between the simulated output and reference signal.

- e Click Update reference signal data.
- **f** In the **Specify Signal to Track Reference Signal** area, select the check-box corresponding to the signal you selected in the previous step, and click **OK**.

Create Requirement		×
	Signal Tracking	
	Specify a tracking requirement on a signal.	
Name: ref_sig		
▼ Specify Refere	nce Signal	
Time vector:	48.9949748743719;49.2462311557789;49.4974874371859;49.748743718593;	50]
Amplitude:	92734535995918;0.992914811096355;0.993090613101637;0.9932620530009	15]
	Update reference signal data	
Tracking Method:	SSE 💌	
🔲 Use robust cos	it	
▼ Specify Signal t	to Track Reference Signal	
	Signal	
✓ PlantOut	put (sldo_model1/Plant:1)	
	-	
🔽 Create Plot	OK Cancel Hel	р
	43	.:

A new reference signalref_sig is created and appears in the **Data** area. The Response Optimization window updates to plot the reference signal.



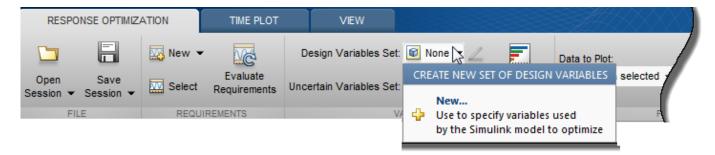
Specify Design Variables

When you optimize the model response, the software modifies the design variable values to meet the design requirements.

In the **Response Optimization** tab:

1 Create a new set of design variables.

In the Design Variables Set drop-down list select New.



The Create Design Variables Set window shows model parameters that you can use as design variables and indicates their locations within the model subsystems.

reate Design Variables Set Create Design Variables set: [DesignVars									
Variable Value Minimum Maximum Scale						Variable	Current value	Used By		
						Kd	0	sldo_model1/Controller		
						Ki	0	sldo_model1/Controller		
Add model variables to optimize.						Кр	1	sldo_model1/Controller		
Adding		s to optim	120.			w0	0.5	sldo_model1/Plant/Transfer Fcn		
						zeta	0.5	sldo_model1/Plant/Transfer Fcn		
	Update model variables									
Variable Detail						Specify expression indexing if necessary (e.g., a(3) or s.x.)				
			ОК							

2 Add parameters to the design variables set.

Select Kd, Ki, and Kp, and click to add the selected parameters.

C	Create Design Variables Set											
(Create D	esign Variables set: [DesignVars									
		Variable	Value	Minimum	Maximum	Scale						
	v	Kd	0	-Inf	Inf	1						
	V	Ki	0	-Inf	Inf	1						
	V	Кр	1	-Inf	Inf	1						

The design variables list displays the following parameter settings:

- Variable Parameter name
- Value Current parameter value
- Minimum and Maximum Parameter bounds
- **Scale** Scaling factor for the parameter
- **3** Limit the parameters to positive values. To do so, enter **0** for the minimum value of each parameter in the corresponding **Minimum** field, and press **Enter** on your keyboard.

Create Design Variables Set										
Create Design Variables set: DesignVars										
	Variable	Value	Minimum	Maximum	Scale					
V	Kd	0	0	Inf	1					
V	Ki	0	0	Inf	1					
V	Кр	1	0	Inf	1					

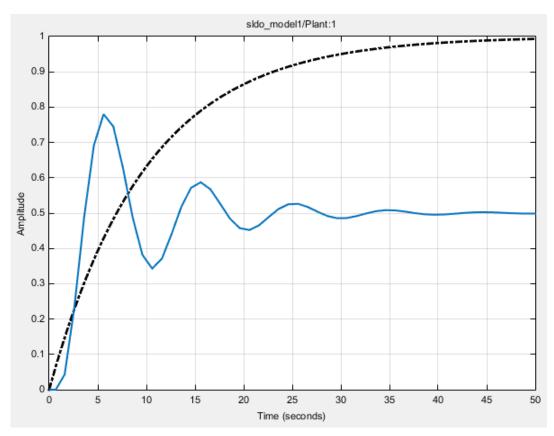
Click **OK**. A new design variable **DesignVars** is created and appears in the **Data** area of the **Response Optimizer**.

 Model Works 	pace (s	ldo_model1)	
Name 🔺		Value	
🕂 Kd		0	
🕂 Ki		0	
🕂 Кр		1	-
▼ Data			
Name 🔺		Value	
DesignVars	3	3x1 Contin	
😰 PlantOutput	5	1x1 Signal	
😰 ref_sig		1x1 Signal	
▼ Variable Previ	ew		
DesignVars(1	,1) =		* II
Name:	'Kd'		
Value:	0		
Minimum:	0		
Maximum:	Inf		
Free:	1		
Scale:	1		-

Optimize Model Response



To view the current model response, click Plot Model Response.



The plot shows that the model response does not track the reference signal.

Click **Optimize**.

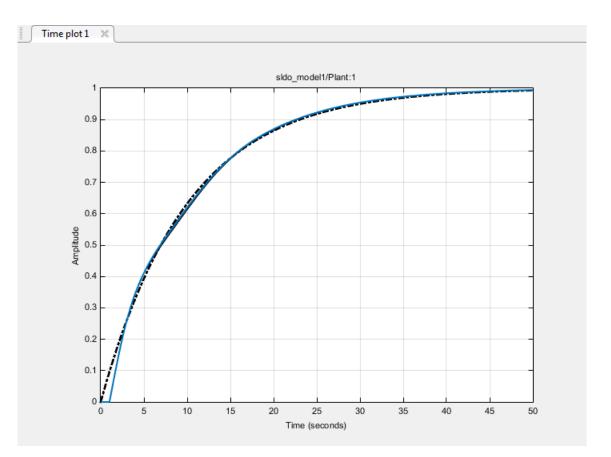
2

At each iteration, the optimization solver Gradient descent (fmincon) modifies the controller parameters to minimize the error between the simulated response and the reference signal. To learn more, see "How the Optimization Algorithm Formulates Minimization Problems".

The message Optimization converged in the Optimization Progress Report indicates that the optimization method found a solution that tracks the reference signal within the tolerances and parameter bounds. For more information about the outputs displayed in the Optimization Progress Report, see "Iterative Display".

Iteration	F-count	ref_sig (Minimize)	
0	5	30.1990	4
1	34	24.6634	Π
2	43	21.3975	
3	51	1.6576	
4	62	1.4586	=
5	71	0.5713	
6	82	0.5114	
7	90	0.3615	
8	98	0.3187	
9	106	0.3148	
10	114	0.3139	
11	122	0.3111	
12	130	0.3047	-
		9-Sep-2014 18:06:45	
Optimizati	on converg	ed, 09-Sep-2014 18:07:25	

3 Verify that the response tracks the reference signal by observing the amplitude versus time plot.



The optimized response closely tracks the reference signal.

4 To view the optimized parameter values, click DesignVars in the Data area of the Response Optimizer. View the updated values in the Variable Preview area.

The optimized values of the design variables are automatically updated in the Simulink model.

See Also

Related Examples

- "Design Optimization to Meet Step Response Requirements (GUI)" on page 3-3
- "Design Optimization to Meet Step Response Requirements (Code)" on page 3-14

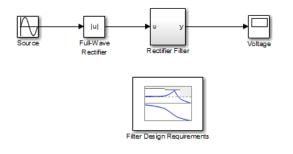
Design Optimization Using Frequency-Domain Check Blocks (GUI)

This example shows how to optimize model parameters to meet frequency-domain requirements using the **Response Optimizer**. Simulink Control Design software must be installed to optimize a design to meet frequency-domain design requirements.

In this example, you specify the design requirements in a Check Bode Characteristics block. You optimize rectifier filter parameters to meet gain and bandwidth requirements by minimizing a custom objective.

Model Structure

The model sdorectifier includes the following blocks:



- Full-Wave Rectifier block An Abs block
- Rectifier Filter subsystem RLC filter implemented using integrator and gain blocks
- Filter Design Requirements block Check Bode Characteristics block that specifies the gain and bandwidth design requirements

Design Requirements

The design optimization problem has several objectives. The design must:

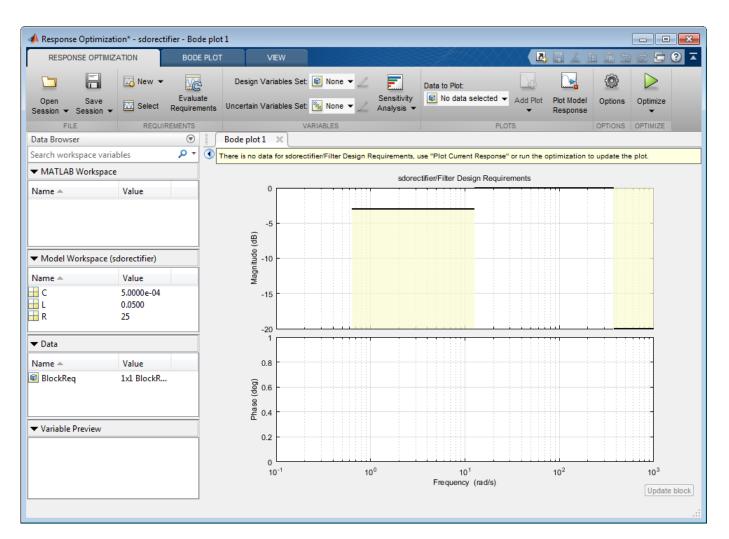
- Have a -3 dB bandwidth of at least 2 Hz
- Limit the gain across the frequency range 2 Hz 60 Hz to at most 0 dB
- Limit the gain above 60 Hz to at most -20 dB
- Maximize the filter resistance R
- Minimize the filter inductance L

The requirements ensure that the rectifier filter combination has minimal high frequency content, responds quickly to voltage changes, and limits filter currents.

Specify Design Requirements

1 Open the **Response Optimizer** for the model.

```
sdotool('sdorectifier')
```



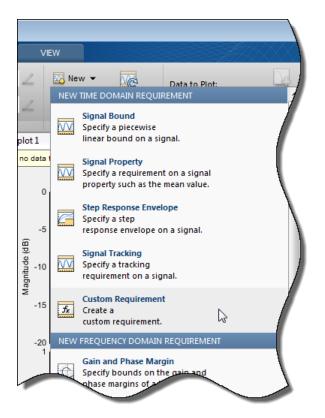
The **Bode plot 1** tab shows the gain and bandwidth requirements specified in the Filter Design Requirements block in the model. To see their values, double-click the block to open the Block Parameters dialog box, and select the **Bounds** tab.

2 Specify a custom objective to minimize the filter inductance and maximize the resistance.

The custom objective is already defined in the sdorectifier_cost function. The function accepts the design variables *R* and *L* and returns the objective to be minimized.

Tip Type edit sdorectifier_cost in the command line to view this function.

a In the New drop-down list, select Custom Requirement.



- **b** Specify the following values in the Create Requirement window, and click **OK**:
 - In the Name edit box, enter MaxMinRL.
 - In the Type edit box, select Minimize the function output
 - In the **Function** edit box, enter @sdorectifier_cost. The optimization solver calls the specified function handle.

Create Requ	irement
	Custom Requirement
	e a custom requirement. The optimizer evaluates the specified fur ion passing a structure with fields containing the optimized des and logged simulation results.
Name: Ma	xMinRL
▼ Specify	Function
Туре:	Minimize the function output 👻
Function:	@sdorectifier_cost
	ostraint is violated

A new requirement variable MaxMinRL is created, and appears in the **Data** area in the **Response Optimizer**. The **Iteration plot 1** tab shows the value of MaxMinRL at each iteration during the optimization.

Specify Design Variables

When you optimize the model response, the software modifies the design variable values to meet the design requirements.

1 In the **Design Variables Set** drop-down list, select **New**.



Select C, L, and R in the Create Design Variable Set window. Click to add the selected parameters to a design variables set.

Cre	eate Design Variables Set								×
Ci	eate Design Variables set:	DesignVars							
Variable Value Minimum Maximum					Scale		Variable	Current value	Used By
	Add mc	odel variable	es to optimi	ze.			C L	0.0005	sdorectifier/Rectifier Filter/1//CL sdorectifier/Rectifier Filter/1//CL1 sdorectifier/Rectifier Filter/1//RC sdorectifier/Rectifier Filter/1//CL sdorectifier/Rectifier Filter/1//CL1
L	Update model variables]	R		sdorectifier/Rectifier Filter/1//RC	
Variable Detail		industes.	J	Specify expression	ession indexing	if necessary (e.g., a(3) or s.x)			

- 2 Specify the value range for each design variable, and click **OK**:
 - C in the range 1μ F-1 mF
 - L in the range 1-500 mH
 - R in the range 0.01–50 ohms

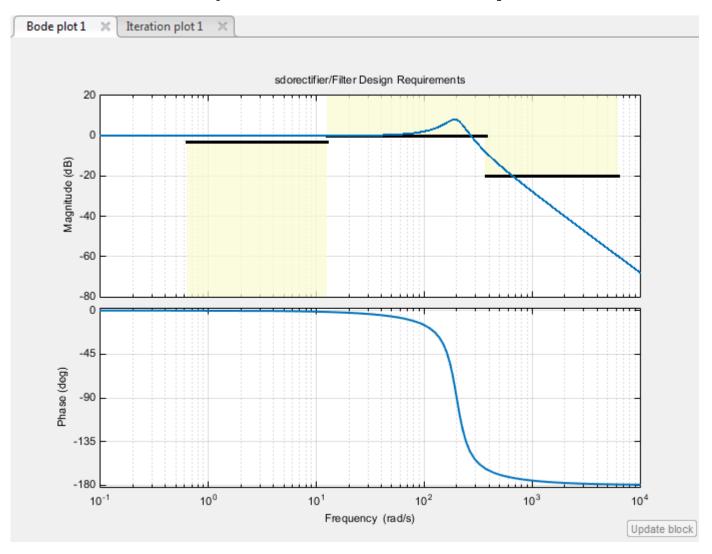
¢	Create De	esign Variables Set 👘								
	Create D	esign Variables set:	DesignVars							
		Variable Value Mir			Maximum	aximum Scale Variable (Current value		
	V	С	0.0005	1e-6	1e-3	0.000976				
	V	L	0.05	1e-3	500e-3	0.0625				
	V	R	25	0.01	50	32				
				Up	j					
	► Varia	ble Detail						Specify expr	ession indexing	if neces:

A new variable DesignVars is created, and appears in the Data area of the Response Optimizer.

Optimize Design

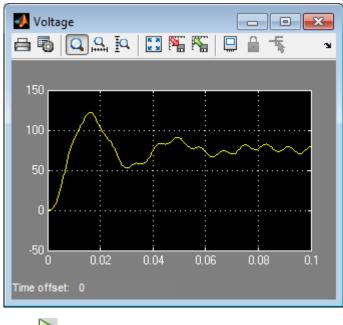
1

To view the current response of the model, click **Plot Model Response**.



The **Bode plot 1** window in the **Response Optimizer** shows that the model output goes out of the region bounded by the design requirement line segments.

In the Voltage scope window, you see that the filter voltage signal overshoots its steady-state value and contains significant harmonic content.

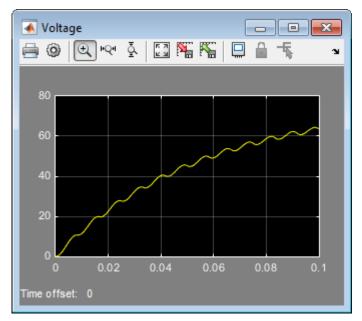


2 Click **Optimize**.

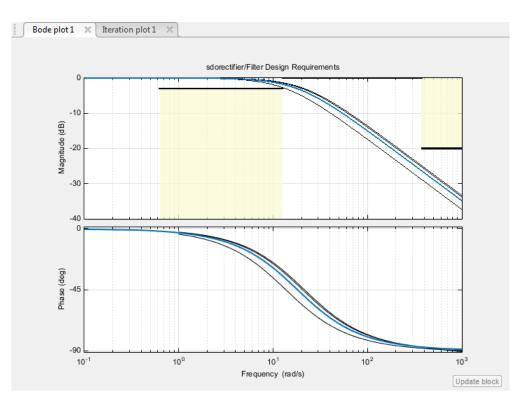
The **Optimization converged** message in the Optimization Progress Report indicates that the optimization method found a solution to satisfy the filter bandwidth requirements.

Iteration	F-count	CustomReq (Minimize)	Filter Design Requireme (<=0)	Filter Design Requireme (>=0)					
0	8	1.5813	8.1361	1.0067					
1	17	1.0970	0.3235	1.0000					
2	26	1.5792	-0.2588	0.6625					
3	34	1.2385	-0.1811	0.7478					
4	45	0.8803	0.0074	0.8924					
5	56	0.8611	-0.1050	0.8608					
6	65	0.8167	-0.0634	0.8539					
7	74	0.4039	-0.3095	0.6692					
8	83	0.1967	-0.5002	0.2846					
9	93	0.0714	-0.3137	0.5628					
10	101	0.0166	-0.3731	0.4406					
11	102	0.0166	-0.3731	0.4406					
Optimizati	11 102 0.0100 -0.5751 0.4400 Iptimization started 24-Sep-2014 15:24:16 Image: Constraint of the start o								

The harmonic content in the filter voltage signal is reduced from the initial design.



3 Verify that the model meets the gain and bandwidth requirements.



The plot displays the output of the last five iterations. The final response using the optimized parameter values appears as the thick blue line.

The optimized response lies in the white region bounded by the design requirement line segments and thus meets the requirements.

4 Click DesignVars in the Data area and view the updated values in the Variable Preview area.

The optimized values of the design variables are automatically updated in the Simulink model.

See Also

Check Bode Characteristics

Related Examples

• "Design Optimization to Meet Frequency-Domain Requirements (GUI)"

Time-Domain Model Verification

This example shows how to perform time-domain model verification using Simulink Design Optimization **Model Verification** blocks. During time-domain verification, the software monitors a signal to check if it meets time-domain characteristics such as step response characteristics and upper and lower amplitudes, or tracks a reference signal.

You can also use blocks from Simulink and Simulink Control Design **Model Verification** libraries to design complex assertion logic for time-domain and frequency-domain verification, and signal monitoring. You can construct simulation tests for your model using the Verification Manager in the Signal Builder.

1 Open Simulink model.

```
sys = 'sldo_model1_stepblk';
open_system(sys);

Unit Step
Controller
Plant
Plant
Step Reports
Step Reports
```

The model includes a Step Response block which is a Check Step Response Characteristics block from the Simulink Design Optimization **Model Verification** library and has default step response bounds.

😼 Sink Block Parameters: Ch	eck Step Response Chara	cteristics	—						
Check Step Response Characteristics									
Assert that the input signal satisfies bounds specified by step response characteristics.									
Bounds Assertion									
☑ Include step response bound in assertion									
Step time (seconds):	0]							
Initial value:	0	Final value:	1						
Rise time (seconds):	5	% Rise:	80						
Settling time (seconds):	7	% Settling:	1						
% Overshoot:	10	% Undershoot:	1						
✓ Enable zero-crossing detection									
Show Plot Show plot	t on block open		Response Optimization						
0	ОК	Cancel	Help Apply						

2 In the Simulink Editor, under **Simulation**, click **Run**.

The block asserts multiple times during simulation because the signal to which the block is connected violates the specified bounds. Assertion warnings appear in the MATLAB command window.

You can optimize model parameters to satisfy the bounds and eliminate assertion warnings. See "Design Optimization to Meet Step Response Requirements (GUI)" on page 3-3.

Optimization-Based Linear Control Design

- "When to Use Optimization-Based Linear Control Design" on page 4-2
- "Types of Time- and Frequency-Domain Design Requirements for Optimization-Based Control Design" on page 4-3
- "Design Optimization-Based PID Controller for Linearized Simulink Model (GUI)" on page 4-4

When to Use Optimization-Based Linear Control Design

When you have Control System Toolbox software installed, you can design and optimize control systems for LTI models by optimizing controller parameters in the **Control System Designer** app. To use optimization methods for linear control design, also known as optimization-based tuning, you must already have an initial controller. You can then use optimization-based tuning to refine the controller design to meet additional design requirements. For more information on designing controllers, see the Control System Toolbox documentation.

Note Optimization-based tuning only changes the value of the controller parameters and not the controller structure itself.

Optimization-based tuning provides flexibility in terms of specifying additional design requirements for the controller. When you have a large number of design requirements, you can first design an initial controller by selecting a subset of requirements and subsequently select additional requirements to refine the design.

Optimization-based tuning also provides flexibility in terms of selecting a subset of controller parameters to optimize, and specifying bounds on the controller parameters.

To design linear controllers for Simulink models using optimization-based tuning, you must first linearize the model using the Simulink Control Design software. For more information on linearizing Simulink models, see the Simulink Control Design documentation.

See Also

Related Examples

- "Optimize LTI System to Meet Frequency-Domain Requirements"
- "Design Optimization-Based PID Controller for Linearized Simulink Model (GUI)" on page 4-4

Types of Time- and Frequency-Domain Design Requirements for Optimization-Based Control Design

When you design linear controllers for LTI or Simulink models using the Simulink Design Optimization software, you can specify both time- and frequency-domain requirements on the system response. You can specify design requirements on the following plots:

- Root Locus plot
- Open-Loop and Prefilter Bode plots
- Open-Loop Nichols plot
- Step/Impulse Response plots

For more information, see "Time- and Frequency-Domain Requirements in Control System Designer App".

Simulink Design Optimization software uses the frequency-domain requirements to compute the frequency response of the system. It then uses optimization methods to reduce the distance between the current response and the requirements by modifying the controller parameters. The software does not change the controller structure when optimizing the controller parameters.

Design Optimization-Based PID Controller for Linearized Simulink Model (GUI)

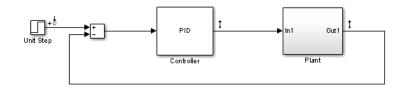
This example shows how to perform optimization-based control design in the **Control System Designer** app when you have Control System Toolbox software. You design a PID controller for a linearized Simulink model.

You accomplish the following tasks:

- Specify frequency-domain Bode magnitude and phase margin requirements.
- Design an initial controller to meet the frequency-domain requirements.
- Refine the initial controller design to limit the controller output signal.

Model Structure

The Simulink model, sldo_model2, contains a Controller block, which is a PID Controller. This block controls the output of the Plant subsystem.



Using the Simulink Control Design software, the model has been linearized at the operating point specified in the model. The sldo_model2.mat file contains a preconfigured **Control System Designer** app session, saved after linearizing the model. To learn more about linearizing Simulink models for control design, see "Control System Design and Tuning" (Simulink Control Design).

The Plant subsystem is modeled as a second-order system with delay. It contains Transfer Function and Transport Delay blocks.



To learn more about the blocks, see the Transfer Fcn and Transport Delay block reference pages.

Design Requirements

The compensator you design must meet the following design requirements:

- Bode lower magnitude bound of 0 in the frequency range 1e-3 to 1 rad/sec
- Phase margin greater than 60 degrees
- Controller output bounds in the range [-250 550]

Configure the Control System Designer App for Optimization-Based Control Design

To design a linear controller for a Simulink model, first configure a **Control System Designer** app session.

1 Open a **Control System Designer** app session for the linearized Simulink model.

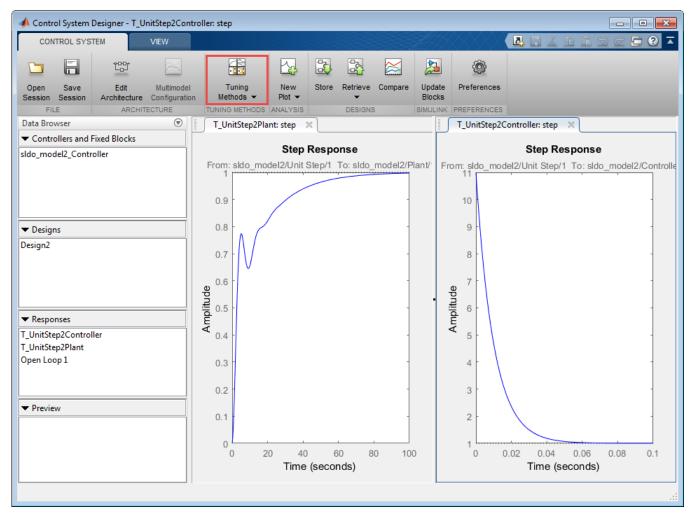
Type the following command at the MATLAB prompt:

controlSystemDesigner('sldo_model2.mat')

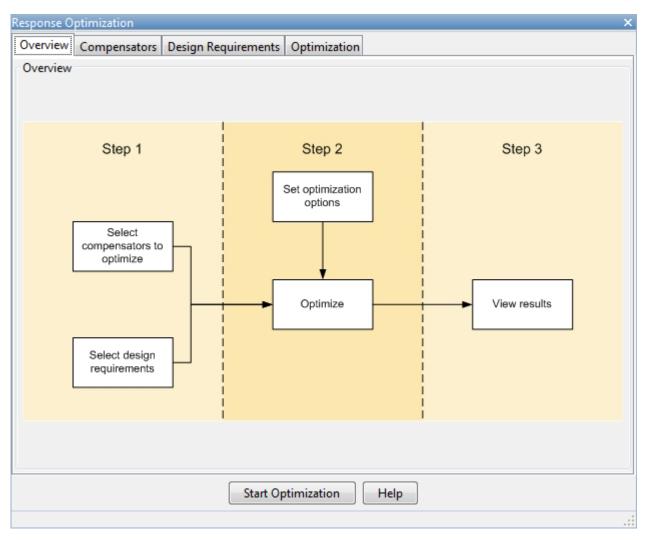
sldo_model2.mat file contains a preconfigured Control System Designer app session. This
session was saved after Simulink Control Design software linearized sldo_model2.

The **Control System Designer** app opens with the following plots:

- Closed-loop step response of the system
- Output of the Controller block



2 To perform response optimization, in the Tuning Methods drop-down list, select Optimization Based Tuning. In the Response Optimization window, you can specify controller parameters and design requirements, and perform optimization.



Design an Initial PID Controller to Meet Bode Magnitude and Phase Margins Requirements

Specify the Controller Parameters

To specify the controller parameters that are to be optimized:

1 In the Response Optimization window, select the **Compensators** tab.

Select compensators to optimize								
🔲 Optimize	Compensator elements	Value	Initial guess	Minimum	Maximum	Typical valu		
	sldo_model2/Controller							
	Gain	0.1	0.1	-Inf	Inf	0.1		
	Real Zero	-8.999	-8.999	-Inf	Inf	-8.999		
	Real Zero	-0.10102	-0.10102	-Inf	Inf	-0.10102		
	Real Pole	-100	-100	-Inf	Inf	-100		

The **Compensators** tab displays the following parameter settings:

- Value Current controller parameter value
- Initial Guess Initial controller parameter value
- Minimum and Maximum Controller parameter bounds
- Typical Value Scaling factor for the controller parameter

Note Compensator elements or parameters cannot have uncertainty when used with frequencydomain based response optimization.

The controller parameters appear as poles and zeros in the **Compensator elements** column:

- Gain Overall gain of the controller
- Real zeros Zeros resulting from the differentiator and integrator
- Real pole Pole resulting from the low-pass filter of the differentiator

Tip To view the structure of the **Controller** block, right-click the block in the model, and select **Mask > Look Under Mask**.

2 Change the PID controller parameters to Simulink block mask parameters format.

Right-click the **sldo_model2/Controller** row, and select **Parameterized format**.

Response Optimiz	zation								
Overview Compensators Design Requirements Optimization									
Select compens	ators to op	timize							
Optimize	nize Compensator elemen			Value	Initial guess				
	sldo_mode	12/Controller							
	Gain			Zero format	0.1	-			
	Real Zero		Parar	meterized form	at _8.999	7			
	Real Zero		20	-0.10102	-0.10102				
	Real Pole			-100	-100				
		_				\leq			

The controller parameters now display as Simulink block mask parameters, P, I, and D. For more information, see "Design Linear Controllers for Simulink Models". To learn more about mask parameters, see "Mask Parameters".

Overview Compensators Design Requirements Optimization									
Select compensators to optimize									
Optimize	Compensator elements	Value	Initial guess	Minimum	Maximum	Typical value			
	sldo_model2/Controller								
	Р	1	1	-Inf	Inf	1			
	I	0.1	0.1	-Inf	Inf	1			
	D	0.1	0.1	-Inf	Inf	1			
	Ν	100	100	-Inf	Inf	1			

3 Select the controller parameters to optimize.

In the **Optimize** column, select P, I, and D.

Response Optimization ×									
Overview Compensators Design Requirements Optimization									
Select compensators to optimize									
Optimize	Compensator elements	Value	Initial guess	Minimum	Maximum	Typical value			
sldo_model2/Controller									
V	Р	1	1	-Inf	Inf	1			
V	I	0.1	0.1	-Inf	Inf	1			
V		0.1	0.1	-Inf	Inf	1			
	N	100	100	-Inf	Inf	1			
		_	_						

Specify Bode Magnitude and Phase Margin Design Requirements

Specify the Bode magnitude lower limit requirement:

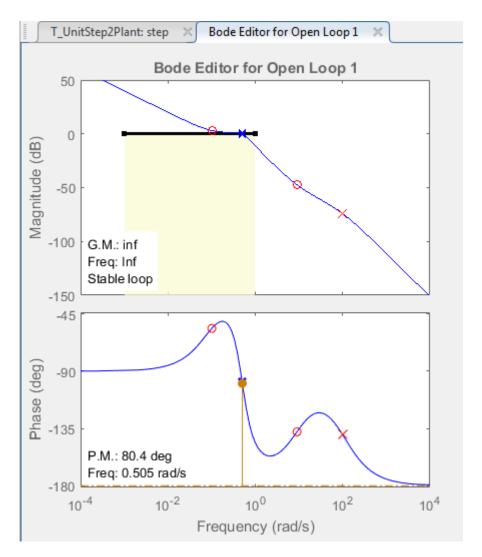
- 1 In the **Design requirements** tab, click **Add new design requirement**. A New Design Requirement dialog box opens.
- 2 In the New Design Requirement dialog box, in the **Design requirement type** drop-down list, select Bode magnitude lower limit.
- 3 In the **Requirement for response** drop-down list, select **Open Loop 1**.
- 4 Specify the **Frequency** range as 1e-3 to 1.
- **5** Specify the **Magnitude** range as 0 to 0.
- 6 Click OK.

📣 New Desig	n Requiremer	nt				• 🗙			
Design requir	ement type:	Bode magnitude lower limit 🔹							
Requirement for response: Open Loop 1									
Design requ	Design requirement parameters								
Type: Cons	train system t	o be >= the	bound 👻						
Edg	e Start	Edge	e End						
Freq. (rad	Mag. (db)	Freq. (rad	Mag. (db)	Slope (dB	Weight	+			
1.0000e-03	0	1	0	0	1				
						1			
				ок	Cancel	Help			

The Bode lower magnitude limit is added to the **Design requirements** tab.

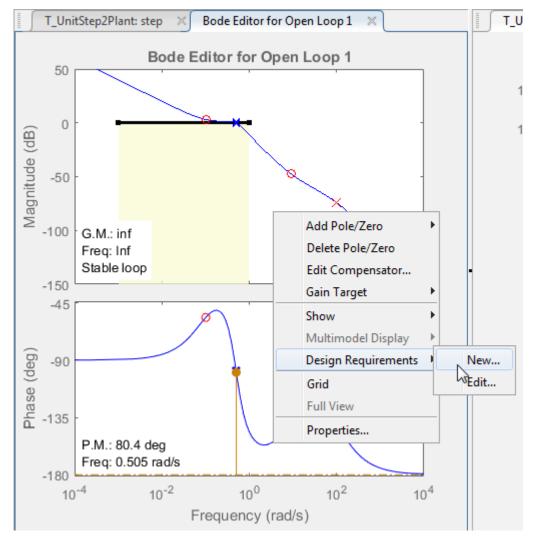
Response Optimizati	on	×							
Overview Compensators Design Requirements Optimization									
Select design requi	irement to satisfy								
Optimize	e Response plot Design requirement								
	Open Loop 1								
	Bode Editor for Open Loop 1	Lower gain limit from 0.001 to 1 (rad/s)							

The **Control System Designer** app window updates to show the Bode plot in a **Bode Editor**. The design requirement is displayed as the black line segment.



Specify the phase margin requirement:

1 Right-click within the white space of the Bode plot, and select **Design Requirements** > **New** to open the New Design Requirement dialog box.



- 2 In the New Design Requirement dialog box, in the **Design requirement type** drop-down list, select Gain & phase margins.
- **3** Select the **Phase margin** check box, and specify the phase margin as 60.

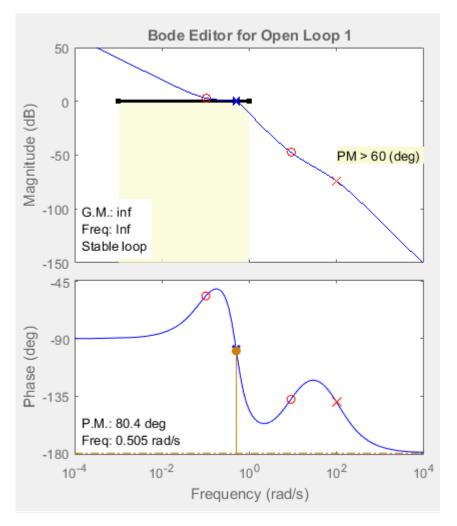
📣 New Design Requir	ement 🗖	×						
Design requirement type: Gain & Phase margins 👻								
Design requirement parameters								
🔲 Gain margin >	20	dB						
🔽 Phase margin >	60	deg						
Ok Close Help								

4 Click OK.

In the Response Optimization window, the **Design requirements** tab updates to display the phase margin requirement.

Overview Compe	nsators Design Requirements Optimization							
Select design requirement to satisfy								
Optimize	Response plot	Design requirement						
	Open Loop 1							
V	Bode Editor for Open Loop 1	Lower gain limit from 0.001 to 1 (rad/s)						
1	Bode Editor for Open Loop 1	PM > 60 (deg)						

In the app, in the Bode Editor, the plot updates to display the phase margin requirement.



Design the Controller

To design the controller with specified design requirements:

1 In the Response Optimization window, in the **Optimization** tab, click **Start Optimization**.

At every optimization iteration, the default optimization method, Gradient descent, reduces the distance between the current response and the magnitude requirement line segment by modifying the controller parameters. Simultaneously, the software also computes the phase margin and reduces the distance between the current response and the phase margin. To learn more about the available optimization methods, click **Optimization Options**, and then click **Help** in the Options dialog box.

After the optimization completes, the **Optimization** tab displays the optimization iterations and status.

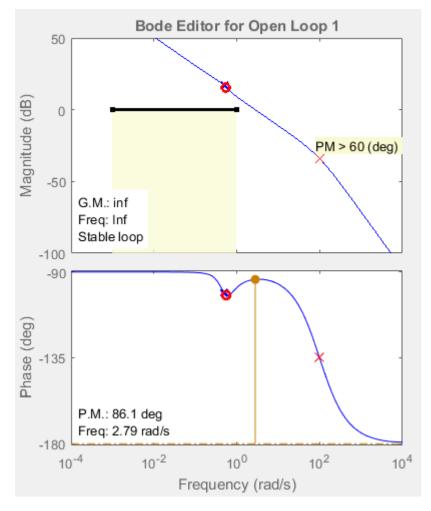
Response Optimizat	tion						x
Overview Comp	ensators Design	Requirements (Optimization				
Optimization Pro	gress						
Iteration	Eval-Count	Cost function	Constraint vio	Step size	Procedure		Optimization options
0	7						
1	14		Display options				
2	21						
3	28						
Optimization starte Optimization finish Successful termine	nization problem ed 02-Dec-2015 17 hed 02-Dec-2015 1 ation. or optimal solution v		*				
		ſ			٦		
			Start Optimization	on Help			

The status message, Successful termination, indicates that the optimization method found a solution that meets the design requirements. For more information about the outputs displayed in the **Optimization progress** table, see "Iterative Display".

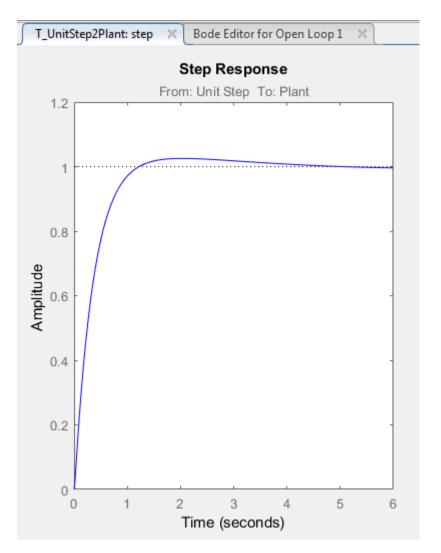
- **2** Examine the controller parameters and the system response:
 - **a** In the **Compensator** tab, view the optimized parameter values in the **Value** column.

Response Op	otimization							X		
Overview	Compensators	Design Requirements	Optin	nization						
Select compensators to optimize										
🔲 Optim	nize C	ompensator elements		Value	Initial guess	Minimum	Maximum	Typical value		
	sldo_model2/Controller									
V	P			6.7627	1	-Inf	Inf	1		
V	I			3.4445	0.1	-Inf	Inf	1		
V	D			11.106	0.1	-Inf	Inf	1		
	N			100	100	-Inf	Inf	1		
Right click on a compensator name to change its representation.										
							Use Value as I	nitial guess		
				ptimization	Help					

- **b** Examine the system response on the following plots:
 - The Bode plot:

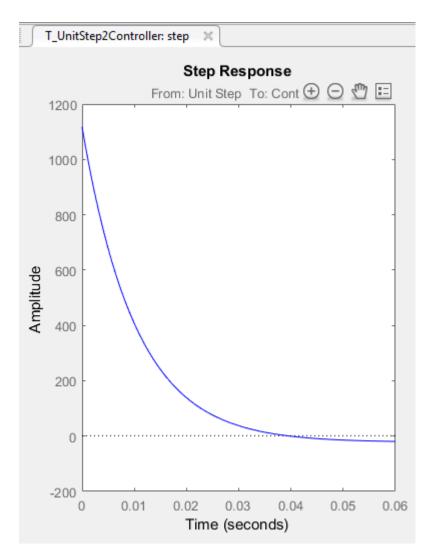


- The magnitude of the system, displayed as the blue curve in the top plot, lies outside the yellow region. This indicates that the system has met the Bode magnitude requirement.
- The phase plot displays the phase margin (P.M.) value of 86.1 degrees. This indicates that the system has met the phase margin design requirement of greater than 60 degrees.
- Closed-loop step response of the system:



The plot shows that the closed-loop response of the system is stable. The system with the designed controller thus meets both the magnitude and phase margin requirements.

• Output of the Controller block:

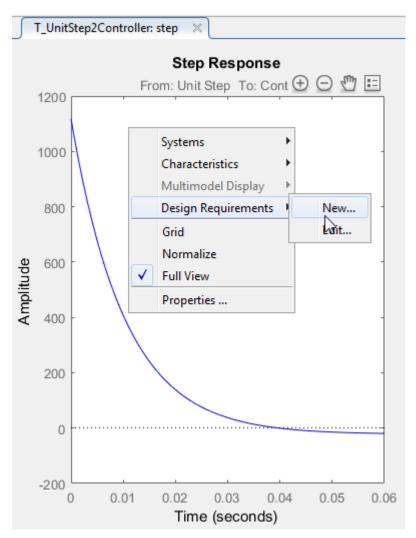


The plot shows that the peak value of the controller output is about 1100, which is large and can damage the plant. To limit the controller output, apply lower and upper bounds on the signal, as specified in "Design Requirements" on page 4-4.

Refine the Controller Design to Meet Controller Output Bounds

To tune the compensator parameters to meet the bounds on the controller output:

- **1** Add an upper-bound on the controller output:
 - a In the controller output plot, right-click the white area, and select **Design requirement** > **New**.

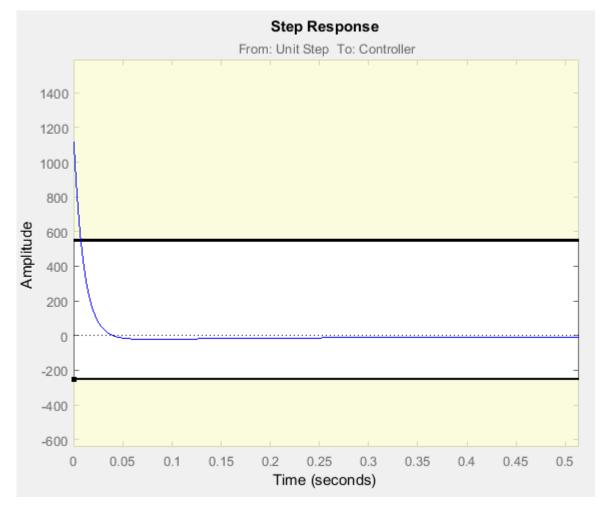


- **b** In the New Design Requirement dialog box, in the **Design requirement type** drop-down list, select Upper time response bound.
- c Specify the **Time** range as 0 to Inf.
- d Specify the Amplitude range as 550 to 550.
- e Click OK.
- 2 Add a lower-bound on the controller output:
 - a In controller output plot, right-click the white area, and select **Design requirement > New**.
 - **b** In the New Design Requirement dialog box, in the **Design requirement type** drop-down list, select Lower time response bound.
 - c Specify the Time range as 0 to Inf.
 - d Specify the Amplitude range as -250 to -250.
 - e Click OK.

In the Response Optimization window, the **Design requirements** tab updates to display the bounds on the controller output.

elect design red	quirement to satisfy							
Optimize Response plot Design requirement								
	Open Loop 1							
V	Bode Editor for Open Loop 1	Lower gain limit from 0.001 to 1 (rad/s)						
V	Bode Editor for Open Loop 1 PM > 60 (deg)							
	T_UnitStep2Controller							
V	Step Response	Upper time response bound from 0 to 10						
V	Step Response	Lower time response bound from 0 to 10						

The plot of the output of the Controller block displays the new design requirements.



3 Optimize the parameters to meet the design requirements on the controller output:

a In the Response Optimization window, in the **Compensators** tab, select the rows containing P, I, and D, and click **Use Value as Initial Guess**.

Select compensators to optimize Optimize Compensator elements Value Initial guess Minimum Maximum Typical									
sldo_model2/Controller									
V	Р		6.7627	1	-Inf	Inf	1		
✓			3.4445	0.1	-Inf	Inf	1		
	D		11.106	0.1	-Inf	Inf	1		
			-Inf	Inf	1				
	N		100	100			-		

The values in the **Initial Guess** column update. When you run the optimization again, the optimization method uses the updated parameter values as the starting point for refining the values.

	Select compensators to optimize								
☑ P 6.7627 6.7627 -Inf Inf 1 ☑ I 3.4445 3.4445 -Inf Inf 1	🗇 Optim Compensator elements Value Initial gu Minimum Maximum Typic								
☑ I 3.4445 3.4445 -Inf Inf 1		sldo_model2/Controller							
	V	P	6.7627	6.7627	-Inf	Inf	1		
11106 11106 Inf Inf 1			3.4445	3.4445	-Inf	Inf	1		
	\checkmark	D	11.106	11.106	-Inf	Inf	1		
N 100 100 -Inf Inf 1		N	100	100	-Inf	Inf	1		

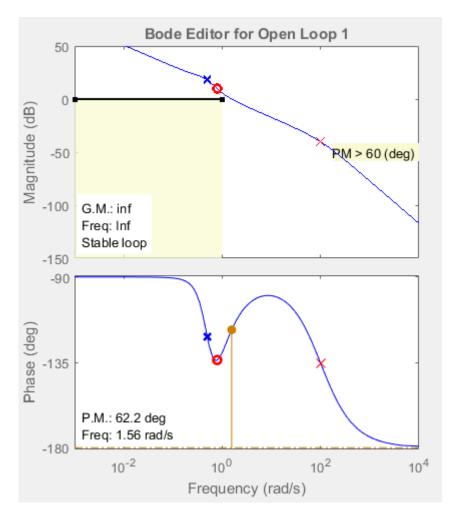
b In the **Optimization** tab, click **Start Optimization**. At every optimization iteration, the optimization method reduces the distance between the current response and the upper and lower bounds on the signal. After the optimization completes, the **Optimization** tab displays the optimization iterations and status.

Overview Compensators Design Requirements Optimization Optimization Progress Iteration Eval-Count Cost func Constrain Step size Procedure Optimization options 0 14 0 1.031 Image: constraint option option constraint optin constraint option constraint optin constraint option	esponse O	ptimization						>
Iteration Eval-Count Cost func Constrain Step size Procedure 0 14 0 1.031	Overview	Compensators	Design Requ	uirements	Optimization			
0 14 0 1.031 Image: Construction of the specified tolerances in the specified tolerances. 0 14 0 1.031 Image: Construction of the specified tolerances in the specified tolerances in the specified tolerances. Display options 0 14 0 1.031 Image: Construction of the specified tolerances in the specified tolerances in the specified tolerances in the specified tolerance in t	Optimizat	ion Progress			,			
1 28 0 0 5.67 Display options Display options Display options Constructing optimization problem V V Optimization started 02-Dec-2015 17:59:58 Optimization finished 02-Dec-2015 18:00:38 V Successful termination. Found a feasible or optimal solution within the specified tolerances. V	Iteratio	n Eval-Count	Cost func	Constrain	. Step size	Procedure		Optimization options
Constructing optimization problem Optimization started 02-Dec-2015 17:59:58 Optimization finished 02-Dec-2015 18:00:38 Successful termination. Found a feasible or optimal solution within the specified tolerances.	0	14	0	1.031				
Constructing optimization problem Optimization started 02-Dec-2015 17:59:58 Optimization finished 02-Dec-2015 18:00:38 Successful termination. Found a feasible or optimal solution within the specified tolerances.	1	28	0	0	5.67			Display options
	Optimizat Optimizat Successfu	tion started 02-Dec tion finished 02-De ul termination.	-2015 17:59:58 c-2015 18:00:3	38 the specified		Help	-	

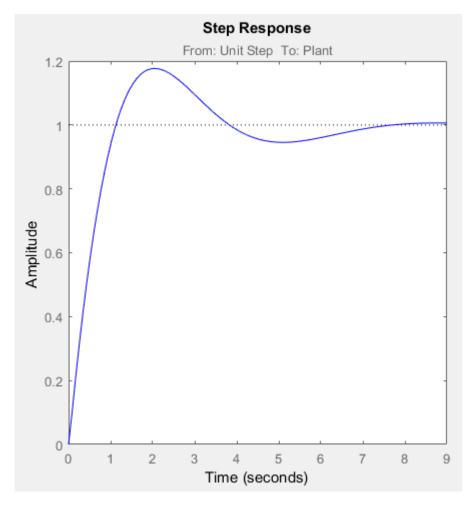
The status message, Successful termination, indicates that the optimization method found a solution that meets the design requirements.

4 Examine the response plots.

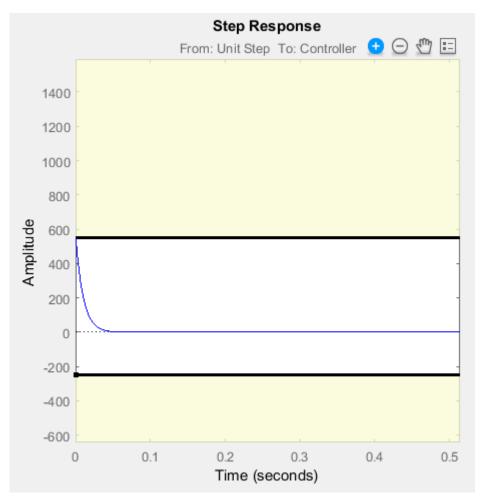
The Bode plots show that after refining the design, the system continues to meet the magnitude and phase margin requirements specified in "Design Requirements" on page 4-4.



Verify that the closed-loop response of the system remains stable after refining the controller design.



The plot of the output of the Controller block shows that the output lies between 550 and -250, and thus meets the design requirement on the bounds of the controller output.



5 Examine the parameter values of the optimized controller.

In the Response Optimization window, in the **Compensators** tab, view the optimized controller parameter values in the **Value** column.

Overview Compensators Design Requirements Optimization									
Select compensators to optimize									
Optim	Compensator elements	Value	Initial gu	Minimum Maximum Typica					
	sldo_model2/Controller								
V	P	6.706	6.7627	-Inf	Inf	1			
V	Ι	3.4445	3.4445	-Inf	Inf	1			
1	D	5.4329	11.106	-Inf	Inf	1			
	N	100	100	-Inf	Inf	1			

6 Write the optimized controller parameter values to the Controller block in the Simulink model.

In the Control System Designer app, click Update Blocks.

📣 Contr	ol System	Designer - T_U	nitStep2Plant: st	tep							
CON	ITROL SYS	тем	VIEW			A			2	<u>~</u> 雪 肁 ·	9 ¢
		면망				2	2	\ge	2	٢	
Open Session	Save Session	Edit Architecture	Multimodel Configuration	Tuning Methods ▼	New Plot 👻	Store	Retrieve •	Compare	Update Blocks	Preferences	
				20010	ANALYSIS		DESIGNS		OMOLINK	PREFERENCES	

7 Save a session with the optimized controller parameters.

In the **Control System Designer** app, select **Save Session**, and specify a name for the session.

See Also

More About

- "Design Linear Controllers for Simulink Models"
- "Optimize LTI System to Meet Frequency-Domain Requirements"